

Package: spatialreg (via r-universe)

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Title Spatial Regression Analysis

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Depends R (>= 3.3.0), spData (>= 2.3.1), Matrix, sf

Imports spdep (>= 1.3-1), coda, methods, MASS, boot, splines, LearnBayes, nlme, multcomp

Suggests parallel, RSpectra, tmap, foreign, spam, knitr, lmtest, expm, sandwich, rmarkdown, igraph (>= 2.0.0), tinytest

Description A collection of all the estimation functions for spatial cross-sectional models (on lattice/areal data using spatial weights matrices) contained up to now in 'spdep'. These model fitting functions include maximum likelihood methods for cross-sectional models proposed by 'Cliff' and 'Ord' (1973, ISBN:0850860369) and (1981, ISBN:0850860814), fitting methods initially described by 'Ord' (1975) <doi:10.1080/01621459.1975.10480272>. The models are further described by 'Anselin' (1988) <doi:10.1007/978-94-015-7799-1>. Spatial two stage least squares and spatial general method of moment models initially proposed by 'Kelejian' and 'Prucha' (1998) <doi:10.1023/A:1007707430416> and (1999) <doi:10.1111/1468-2354.00027> are provided. Impact methods and MCMC fitting methods proposed by 'LeSage' and 'Pace' (2009) <doi:10.1201/9781420064254> are implemented for the family of cross-sectional spatial regression models. Methods for fitting the log determinant term in maximum likelihood and MCMC fitting are compared by 'Bivand et al.' (2013) <doi:10.1111/gean.12008>, and model fitting methods by 'Bivand' and 'Piras' (2015) <doi:10.18637/jss.v063.i18>; both of these articles include extensive lists of references. A recent review is provided by 'Bivand', 'Millo' and 'Piras' (2021) <doi:10.3390/math9111276>. 'spatialreg' >= 1.1-* corresponded to 'spdep' >= 1.1-1, in which the model fitting functions were deprecated and passed through to 'spatialreg', but masked those

in 'spatialreg'. From versions 1.2-*, the functions have been made defunct in 'spdep'. From version 1.3-6, add Anselin-Kelejian (1997) test to `stsls` for residual spatial autocorrelation <doi:10.1177/016001769702000109>.

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URL <https://github.com/r-spatial/spatialreg/>,
<https://r-spatial.github.io/spatialreg/>

BugReports <https://github.com/r-spatial/spatialreg/issues/>

VignetteBuilder knitr

NeedsCompilation yes

RoxygenNote 6.1.1

Config/pak/sysreqs libudunits2-dev

Repository <https://r-spatial.r-universe.dev>

RemoteUrl <https://github.com/r-spatial/spatialreg>

RemoteRef HEAD

RemoteSha 4fb0286416f99d1cf4b08e6d092d6f002b3450f7

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aple *Approximate profile-likelihood estimator (APLE)*

Description

The Approximate profile-likelihood estimator (APLE) of the simultaneous autoregressive model’s spatial dependence parameter was introduced in Li et al. (2007). It employs a correction term using the eigenvalues of the spatial weights matrix, and consequently should not be used for large numbers of observations. It also requires that the variable has a mean of zero, and it is assumed that it has been detrended. The spatial weights object is assumed to be row-standardised, that is using default `style="W"` in `nb2listw`.

Usage

`aple(x, listw, override_similarity_check=FALSE, useTrace=TRUE)`

Arguments

`x` a zero-mean detrended continuous variable
`listw` a `listw` object from for example `spdep::nb2listw`
`override_similarity_check` default FALSE, if TRUE - typically for row-standardised weights with asymmetric underlying general weights - similarity is not checked
`useTrace` default TRUE, use trace of sparse matrix $W \%* \% W$ (Li et al. (2010)), if FALSE, use crossproduct of eigenvalues of W as in Li et al. (2007)

Details

This implementation has been checked with Hongfei Li’s own implementation using her data; her help was very valuable.

Value

A scalar APLE value.

Author(s)

Roger Bivand <Roger.Bivand@nhh.no>

References

Li, H, Calder, C. A. and Cressie N. A. C. (2007) Beyond Moran’s I: testing for spatial dependence based on the spatial autoregressive model. *Geographical Analysis* 39, 357-375; Li, H, Calder, C. A. and Cressie N. A. C. (2012) One-step estimation of spatial dependence parameters: Properties and extensions of the APLE statistic, *Journal of Multivariate Analysis* 105, 68-84.

See Also

[nb2listw](#), [aple.mc](#), [aple.plot](#)

Examples

```
wheat <- st_read(system.file("shapes/wheat.gpkg", package="spData")[1], quiet=TRUE)
library(spdep)
nbr1 <- spdep::poly2nb(wheat, queen=FALSE)
nbr1 <- spdep::nblag(nbr1, 2)
nbr12 <- spdep::nblag_cumul(nbr1)
cms0 <- with(as.data.frame(wheat), tapply(yield, c, median))
cms1 <- c(model.matrix(~ factor(c) -1, data=wheat) %*% cms0)
wheat$yield_detrend <- wheat$yield - cms1
isTRUE(all.equal(c(with(as.data.frame(wheat),
  tapply(yield_detrend, c, median))), rep(0.0, 25),
  check.attributes=FALSE))
spdep::moran.test(wheat$yield_detrend, spdep::nb2listw(nbr12, style="W"))
aple(as.vector(scale(wheat$yield_detrend, scale=FALSE)), spdep::nb2listw(nbr12, style="W"))
## Not run:
errorsar1m(yield_detrend ~ 1, wheat, spdep::nb2listw(nbr12, style="W"))

## End(Not run)
```

aple.mc

Approximate profile-likelihood estimator (APLE) permutation test

Description

A permutation bootstrap test for the approximate profile-likelihood estimator (APLE).

Usage

```
aple.mc(x, listw, nsim, override_similarity_check=FALSE, useTrace=TRUE)
```

Arguments

x	a zero-mean detrended continuous variable
listw	a listw object from for example spdep::nb2listw
nsim	number of simulations
override_similarity_check	default FALSE, if TRUE - typically for row-standardised weights with asymmetric underlying general weights - similarity is not checked
useTrace	default TRUE, use trace of sparse matrix $W \%* \% W$ (Li et al. (2010)), if FALSE, use crossproduct of eigenvalues of W as in Li et al. (2007)

Value

A boot object as returned by the boot function.

Author(s)

Roger Bivand <Roger.Bivand@nhh.no>

References

Li, H, Calder, C. A. and Cressie N. A. C. (2007) Beyond Moran's I: testing for spatial dependence based on the spatial autoregressive model. *Geographical Analysis* 39, 357-375; Li, H, Calder, C. A. and Cressie N. A. C. (2012) One-step estimation of spatial dependence parameters: Properties and extensions of the APLE statistic, *Journal of Multivariate Analysis* 105, 68-84.

See Also

[apple](#), [boot](#)

Examples

```
## Not run:
wheat <- st_read(system.file("shapes/wheat.gpkg", package="spData")[1], quiet=TRUE)
nbr1 <- spdep::poly2nb(wheat, queen=FALSE)
nbr1 <- spdep::nblag(nbr1, 2)
nbr12 <- spdep::nblag_cumul(nbr1)
wheat_g <- wheat
st_geometry(wheat_g) <- NULL
cms0 <- with(wheat_g, tapply(yield, c, median))
cms1 <- c(model.matrix(~ factor(c) -1, data=wheat) %**% cms0)
wheat$yield_detrend <- wheat$yield - cms1
oldRNG <- RNGkind()
RNGkind("L'Ecuyer-CMRG")
set.seed(1L)
boot_out_ser <- apple.mc(as.vector(scale(wheat$yield_detrend, scale=FALSE)),
  spdep::nb2listw(nbr12, style="W"), nsim=500)
plot(boot_out_ser)
boot_out_ser
library(parallel)
oldCores <- set.coresOption(NULL)
nc <- max(2L, detectCores(logical=FALSE), na.rm = TRUE)-1L
# set nc to 1L here
if (nc > 1L) nc <- 1L
invisible(set.coresOption(nc))
set.seed(1L)
if (!get.mcOption()) {
  cl <- makeCluster(nc)
  set.ClusterOption(cl)
} else{
  mc.reset.stream()
}
boot_out_par <- apple.mc(as.vector(scale(wheat$yield_detrend, scale=FALSE)),
  spdep::nb2listw(nbr12, style="W"), nsim=500)
if (!get.mcOption()) {
  set.ClusterOption(NULL)
  stopCluster(cl)
}
```

```

boot_out_par
invisible(set.coresOption(oldCores))
RNGkind(oldRNG[1], oldRNG[2])

## End(Not run)

```

apple.plot

Approximate profile-likelihood estimator (APLE) scatterplot

Description

A scatterplot decomposition of the approximate profile-likelihood estimator, and a local APLE based on the list of vectors returned by the scatterplot function.

Usage

```

apple.plot(x, listw, override_similarity_check=FALSE, useTrace=TRUE, do.plot=TRUE, ...)
localAple(x, listw, override_similarity_check=FALSE, useTrace=TRUE)

```

Arguments

x	a zero-mean detrended continuous variable
listw	a listw object from for example <code>spdep::nb2listw</code>
override_similarity_check	default FALSE, if TRUE - typically for row-standardised weights with asymmetric underlying general weights - similarity is not checked
useTrace	default TRUE, use trace of sparse matrix $W \%* \% W$ (Li et al. (2010)), if FALSE, use crossproduct of eigenvalues of W as in Li et al. (2007)
do.plot	default TRUE: should a scatterplot be drawn
...	other arguments to be passed to plot

Details

The function solves a secondary eigenproblem of size n internally, so constructing the values for the scatterplot is quite compute and memory intensive, and is not suitable for very large n .

Value

apple.plot returns list with components:

X	A vector as described in Li et al. (2007), p. 366.
Y	A vector as described in Li et al. (2007), p. 367.

localAple returns a vector of local APLE values.

Author(s)

Roger Bivand <Roger.Bivand@nhh.no>

References

Li, H, Calder, C. A. and Cressie N. A. C. (2007) Beyond Moran's I: testing for spatial dependence based on the spatial autoregressive model. *Geographical Analysis* 39, pp. 357-375; Li, H, Calder, C. A. and Cressie N. A. C. (2012) One-step estimation of spatial dependence parameters: Properties and extensions of the APLE statistic, *Journal of Multivariate Analysis* 105, 68-84.

See Also

[aple](#)

Examples

```
## Not run:
wheat <- st_read(system.file("shapes/wheat.gpkg", package="spData")[1], quiet=TRUE)
nbr1 <- spdep::poly2nb(wheat, queen=FALSE)
nbr1 <- spdep::nblag(nbr1, 2)
nbr12 <- spdep::nblag_cumul(nbr1)
cms0 <- with(as.data.frame(wheat), tapply(yield, c, median))
cms1 <- c(model.matrix(~ factor(c) -1, data=wheat) %*% cms0)
wheat$yield_detrend <- wheat$yield - cms1
plt_out <- aple.plot(as.vector(scale(wheat$yield_detrend, scale=FALSE)),
  spdep::nb2listw(nbr12, style="W"), cex=0.6)
lm_obj <- lm(Y ~ X, plt_out)
abline(lm_obj)
abline(v=0, h=0, lty=2)
zz <- summary(influence.measures(lm_obj))
infl <- as.integer(rownames(zz))
points(plt_out$X[infl], plt_out$Y[infl], pch=3, cex=0.6, col="red")
crossprod(plt_out$Y, plt_out$X)/crossprod(plt_out$X)
wheat$localAple <- localAple(as.vector(scale(wheat$yield_detrend, scale=FALSE)),
  spdep::nb2listw(nbr12, style="W"))
mean(wheat$localAple)
hist(wheat$localAple)
opar <- par(no.readonly=TRUE)
plot(wheat[, "localAple"], reset=FALSE)
text(st_coordinates(st_centroid(st_geometry(wheat)))[infl,], labels=rep("*", length(infl)))
par(opar)

## End(Not run)
```

as.spam.listw

Spatial neighbour sparse representation

Description

Interface between Matrix class objects and weights lists. The `as.spam.listw` method converts a "listw" object to a sparse matrix as defined in the **spam** package.

Usage

```

as.spam.listw(listw)
listw2U_spam(lw)
listw2U_Matrix(lw)
as_dgRMatrix_listw(listw)
as_dsTMatrix_listw(listw)
as_dsCMatrix_I(n)
as_dsCMatrix_IrW(W, rho)
Jacobian_W(W, rho)
powerWeights(W, rho, order=250, X, tol=.Machine$double.eps^(3/5))

```

Arguments

listw, lw	a listw object from for example nb2listw
W	a dsTMatrix object created using as_dsTMatrix_listw from a symmetric listw object
rho	spatial regression coefficient
n	length of diagonal for identity matrix
order	Power series maximum limit
X	A numerical matrix
tol	Tolerance for convergence of power series

Author(s)

Roger Bivand <Roger.Bivand@nhh.no>

See Also

[nb2listw](#)

Examples

```

## Not run:
require(sf, quietly=TRUE)
columbus <- st_read(system.file("shapes/columbus.gpkg", package="spData")[1], quiet=TRUE)
#require(spdep, quietly=TRUE)
col.gal.nb <- spdep::read.gal(system.file("weights/columbus.gal", package="spData")[1])
col.listw <- spdep::nb2listw(col.gal.nb)
if (require("spam", quietly=TRUE)) {
  col.sp <- as.spam.listw(col.listw)
  str(col.sp)
}
suppressMessages(nyadjmat <- as.matrix(foreign::read.dbf(system.file(
  "misc/nyadjwts.dbf", package="spData")[1])[-1]))
nyadjlw <- spdep::mat2listw(nyadjmat)
listw_NY <- spdep::nb2listw(nyadjlw$neighbours, style="B")
W_C <- as(listw_NY, "CsparseMatrix")
W_R <- as(listw_NY, "RsparseMatrix")

```

```

W_S <- as(listw_NY, "symmetricMatrix")
n <- nrow(W_S)
I <- Diagonal(n)
rho <- 0.1
c(determinant(I - rho * W_S, logarithm=TRUE)$modulus)
sum(log(1 - rho * eigenw(listw_NY)))
nW <- - W_S
nChol <- Cholesky(nW, Imult=8)
n * log(rho) + (2 * c(determinant(update(nChol, nW, 1/rho))$modulus))

## End(Not run)
nb7rt <- spdep::cell2nb(7, 7, torus=TRUE)
x <- matrix(sample(rnorm(500*length(nb7rt))), nrow=length(nb7rt))
lw <- spdep::nb2listw(nb7rt)
if (FALSE) {
# Only needed in some simulation settings where the input and
# output distributions must agree in all but autocorrelation
e <- eigenw(lw)
x <- apply(x, 2, scale)
st <- apply(x, 2, function(x) shapiro.test(x)$p.value)
x <- x[, (st > 0.2 & st < 0.8)]
x <- apply(x, 2, function(v) residuals(spautolm(v ~ 1, listw=lw,
method="eigen", control=list(pre_eig=e, fdHess=FALSE))))
x <- apply(x, 2, scale)
}
W <- as(lw, "CsparseMatrix")
system.time(e <- invIrM(nb7rt, rho=0.98, method="solve", feasible=NULL) %*% x)
system.time(ee <- powerWeights(W, rho=0.98, X=x))
str(attr(ee, "internal"))
all.equal(e, as(ee, "matrix"), check.attributes=FALSE)
## Not run:
system.time(ee <- powerWeights(W, rho=0.9, X=x))
system.time(ee <- powerWeights(W, rho=0.98, order=1000, X=x))
all.equal(e, as(ee, "matrix"), check.attributes=FALSE)
nb60rt <- spdep::cell2nb(60, 60, torus=TRUE)
W <- as(spdep::nb2listw(nb60rt), "CsparseMatrix")
set.seed(1)
x <- matrix(rnorm(dim(W)[1]), ncol=1)
system.time(ee <- powerWeights(W, rho=0.3, X=x))
str(as(ee, "matrix"))
obj <- errorsarlm(as(ee, "matrix")[,1] ~ 1, listw=spdep::nb2listw(nb60rt), method="Matrix")
coefficients(obj)

## End(Not run)

```

Description

These functions are made available in the package namespace for other developers, and are not intended for users. They provide a shared infrastructure for setting up data for Jacobian computation, and then for calculating the Jacobian, either exactly or approximately, in maximum likelihood fitting of spatial regression models. The techniques used are the exact eigenvalue, Cholesky decompositions (Matrix, spam), and LU ones, with Chebyshev and Monte Carlo approximations; moments use the methods due to Martin and Smirnov/Anselin.

Usage

```
do_ldet(coef, env, which=1)
jacobianSetup(method, env, con, pre_eig=NULL, trs=NULL, interval=NULL, which=1)
cheb_setup(env, q=5, which=1)
mcdet_setup(env, p=16, m=30, which=1)
eigen_setup(env, which=1)
eigen_pre_setup(env, pre_eig, which=1)
spam_setup(env, pivot="MMD", which=1)
spam_update_setup(env, in_coef=0.1, pivot="MMD", which=1)
Matrix_setup(env, Imult, super=as.logical(NA), which=1)
Matrix_J_setup(env, super=FALSE, which=1)
LU_setup(env, which=1)
LU_prepermutate_setup(env, coef=0.1, order=FALSE, which=1)
moments_setup(env, trs=NULL, m, p, type="MC", correct=TRUE, trunc=TRUE, eq7=TRUE, which=1)
SE_classic_setup(env, SE_method="LU", p=16, m=30, nrho=200, interpn=2000,
  interval=c(-1,0.999), SEldet=NULL, which=1)
SE_whichMin_setup(env, SE_method="LU", p=16, m=30, nrho=200, interpn=2000,
  interval=c(-1,0.999), SEldet=NULL, which=1)
SE_interp_setup(env, SE_method="LU", p=16, m=30, nrho=200,
  interval=c(-1,0.999), which=1)
can.be.simmed(listw)
```

Arguments

coef	spatial coefficient value
env	environment containing pre-computed objects, fixed after assignment in setup functions
which	default 1; if 2, use second listw object
method	string value, used by jacobianSetup to choose method
con	control list passed from model fitting function and parsed in jacobianSetup to set environment variables for method-specific setup
pre_eig	pre-computed eigenvalues of length n
q	Chebyshev approximation order; default in calling spdep functions is 5, here it cannot be missing and does not have a default
p	Monte Carlo approximation number of random normal variables; default calling spdep functions is 16, here it cannot be missing and does not have a default

<code>m</code>	Monte Carlo approximation number of series terms; default in calling <code>spdep</code> functions is 30, here it cannot be missing and does not have a default; <code>m</code> serves the same purpose in the moments method
<code>pivot</code>	default “MMD”, may also be “RCM” for Cholesky decomposition using <code>spam</code>
<code>in_coef</code>	fill-in initiation coefficient value, default 0.1
<code>Imult</code>	see Cholesky ; numeric scalar which defaults to zero. The matrix that is decomposed is $A+m*I$ where <code>m</code> is the value of <code>Imult</code> and <code>I</code> is the identity matrix of order <code>ncol(A)</code> . Default in calling <code>spdep</code> functions is 2, here it cannot be missing and does not have a default, but is rescaled for binary weights matrices in proportion to the maximum row sum in those calling functions
<code>super</code>	see Cholesky ; logical scalar indicating if a supernodal decomposition should be created. The alternative is a simplicial decomposition. Default in calling <code>spdep</code> functions is <code>FALSE</code> for “Matrix_J” and <code>as.logical(NA)</code> for “Matrix”. Setting it to <code>NA</code> leaves the choice to a <code>CHOLMOD</code> -internal heuristic
<code>order</code>	default <code>FALSE</code> ; used in <code>LU_prepermute</code> , note warnings given for <code>lu</code> method
<code>trs</code>	A numeric vector of <code>m</code> traces, as from <code>trW</code>
<code>type</code>	moments trace type, see trW
<code>correct</code>	default <code>TRUE</code> : use Smirnov correction term, see trW
<code>trunc</code>	default <code>TRUE</code> : truncate Smirnov correction term, see trW
<code>eq7</code>	default <code>TRUE</code> ; use equation 7 in Smirnov and Anselin (2009), if <code>FALSE</code> no unit root correction
<code>SE_method</code>	default “LU”, alternatively “MC”; underlying <code>Indet</code> method to use for generating SE toolbox emulation grid
<code>nrho</code>	default 200, number of <code>Indet</code> values in first stage SE toolbox emulation grid
<code>interval</code>	default <code>c(-1,0.999)</code> if <code>interval</code> argument <code>NULL</code> , bounds for SE toolbox emulation grid
<code>interp</code>	default 2000, number of <code>Indet</code> values to interpolate in second stage SE toolbox emulation grid
<code>SEIndet</code>	default <code>NULL</code> , used to pass a pre-computed two-column matrix of coefficient values and corresponding interpolated <code>Indet</code> values
<code>listw</code>	a spatial weights object

Details

Since environments are containers in the R workspace passed by reference rather than by value, they are useful for passing objects to functions called in numerical optimisation, here for the maximum likelihood estimation of spatial regression models. This technique can save a little time on each function call, balanced against the need to access the objects in the environment inside the function. The environment should contain a family string object either “SAR”, “CAR” or “SMA” (used in `do_ldet` to choose spatial moving average in `spautolm`, and these specific objects before calling the set-up functions:

eigen Classical Ord eigenvalue computations - either:

listw A `listw` spatial weights object

can.sim logical scalar: can the spatial weights be made symmetric by similarity
verbose logical scalar: legacy report print control, for historical reasons only
 or:

pre_eig pre-computed eigenvalues

and assigns to the environment:

eig a vector of eigenvalues

eig.range the search interval for the spatial coefficient

method string: “eigen”

Matrix Sparse matrix pre-computed Cholesky decomposition with fast updating:

listw A listw spatial weights object

can.sim logical scalar: can the spatial weights be made symmetric by similarity
 and assigns to the environment:

csrw sparse spatial weights matrix

nW negative sparse spatial weights matrix

pChol a “CHMfactor” from factorising cswr with [Cholesky](#)

nChol a “CHMfactor” from factorising nW with [Cholesky](#)

method string: “Matrix”

Matrix_J Standard Cholesky decomposition without updating:

listw A listw spatial weights object

can.sim logical scalar: can the spatial weights be made symmetric by similarity
n number of spatial objects

and assigns to the environment:

csrw sparse spatial weights matrix

I sparse identity matrix

super the value of the super argument

method string: “Matrix_J”

spam Standard Cholesky decomposition without updating:

listw A listw spatial weights object

can.sim logical scalar: can the spatial weights be made symmetric by similarity
n number of spatial objects

and assigns to the environment:

csrw sparse spatial weights matrix

I sparse identity matrix

pivot string — pivot method

method string: “spam”

spam_update Pre-computed Cholesky decomposition with updating:

listw A listw spatial weights object

can.sim logical scalar: can the spatial weights be made symmetric by similarity
n number of spatial objects

and assigns to the environment:

csrw sparse spatial weights matrix
I sparse identity matrix
csrwchol A Cholesky decomposition for updating
method string: “spam”

LU Standard LU decomposition without updating:

listw A listw spatial weights object
n number of spatial objects
 and assigns to the environment:
W sparse spatial weights matrix
I sparse identity matrix
method string: “LU”

LU_prepermute Standard LU decomposition with updating (pre-computed fill-reducing permutation):

listw A listw spatial weights object
n number of spatial objects
 and assigns to the environment:
W sparse spatial weights matrix
lu_order order argument to lu
pq 2-column matrix for row and column permutation for fill-reduction
I sparse identity matrix
method string: “LU”

MC Monte Carlo approximation:

listw A listw spatial weights object
 and assigns to the environment:
clx list of Monte Carlo approximation terms (the first two simulated traces are replaced by their analytical equivalents)
W sparse spatial weights matrix
method string: “MC”

cheb Chebyshev approximation:

listw A listw spatial weights object
 and assigns to the environment:
trT vector of Chebyshev approximation terms
W sparse spatial weights matrix
method string: “Chebyshev”

moments moments approximation:

listw A listw spatial weights object
can.sim logical scalar: can the spatial weights be made symmetric by similarity
 and assigns to the environment:
trs vector of traces, possibly approximated
q12 integer vector of length 2, unit roots terms, ignored until 0.5-52

eq7 logical scalar: use equation 7
correct logical scalar: use Smirnov correction term
trunc logical scalar: truncate Smirnov correction term
method string: “moments”

SE_classic :

listw A listw spatial weights object
n number of spatial objects
 and assigns to the environment:
detval two column matrix of lndet grid values
method string: “SE_classic”
SE_method string: “LU” or “MC”

SE_whichMin :

listw A listw spatial weights object
n number of spatial objects
 and assigns to the environment:
detval two column matrix of lndet grid values
method string: “SE_whichMin”
SE_method string: “LU” or “MC”

SE_interp :

listw A listw spatial weights object
n number of spatial objects
 and assigns to the environment:
fit fitted spline object from which to predict lndet values
method string: “SE_interp”
SE_method string: “LU” or “MC”

Some set-up functions may also assign similar to the environment if the weights were made symmetric by similarity.

Three set-up functions emulate the behaviour of the Spatial Econometrics toolbox (March 2010) maximum likelihood lndet grid performance. The toolbox lndet functions compute a smaller number of lndet values for a grid of coefficient values (spacing 0.01), and then interpolate to a finer grid of values (spacing 0.001). “SE_classic”, which is an implementation of the SE toolbox code, for example in `f_sar.m`, appears to have selected a row in the grid matrix one below the correct row when the candidate coefficient value was between 0.005 and 0.01-fuzz, always rounding the row index down. A possible alternative is to choose the index that is closest to the candidate coefficient value (“SE_whichMin”). Another alternative is to fit a spline model to the first stage coarser grid, and pass this fitted model to the log likelihood function to make a point prediction using the candidate coefficient value, rather than finding the grid index (“SE_interp”).

Value

`do_ldet` returns the value of the Jacobian for the calculation method recorded in the environment argument, and for the Monte Carlo approximation, returns a measure of the spread of the approximation as an “sd” attribute; the remaining functions modify the environment in place as a side effect and return nothing.

Author(s)

Roger Bivand <Roger.Bivand@nhh.no>

References

LeSage J and RK Pace (2009) Introduction to Spatial Econometrics. CRC Press, Boca Raton, pp. 77–110.

Bivand, R. S., Hauke, J., and Kossowski, T. (2013). Computing the Jacobian in Gaussian spatial autoregressive models: An illustrated comparison of available methods. *Geographical Analysis*, 45(2), 150-179.

See Also

[spautolm](#), [lagsarlm](#), [errorsarlm](#), [Cholesky](#)

Examples

```
data(boston, package="spData")
#require("spdep", quietly=TRUE)
lw <- spdep::nb2listw(boston.soi)
can.sim <- can.be.simmed(lw)
env <- new.env(parent=globalenv())
assign("listw", lw, envir=env)
assign("can.sim", can.sim, envir=env)
assign("similar", FALSE, envir=env)
assign("verbose", FALSE, envir=env)
assign("family", "SAR", envir=env)
eigen_setup(env)
get("similar", envir=env)
do_ldet(0.5, env)
rm(env)
env <- new.env(parent=globalenv())
assign("listw", lw, envir=env)
assign("can.sim", can.sim, envir=env)
assign("similar", FALSE, envir=env)
assign("verbose", FALSE, envir=env)
assign("family", "SAR", envir=env)
assign("n", length(boston.soi), envir=env)
eigen_pre_setup(env, pre_eig=eigenw(similar.listw(lw)))
do_ldet(0.5, env)
rm(env)
env <- new.env(parent=globalenv())
assign("listw", lw, envir=env)
assign("can.sim", can.sim, envir=env)
assign("similar", FALSE, envir=env)
assign("family", "SAR", envir=env)
assign("n", length(boston.soi), envir=env)
Matrix_setup(env, Imult=2, super=FALSE)
get("similar", envir=env)
do_ldet(0.5, env)
rm(env)
```

```

env <- new.env(parent=globalenv())
assign("listw", lw, envir=env)
assign("n", length(boston.soi), envir=env)
assign("can.sim", can.sim, envir=env)
assign("similar", FALSE, envir=env)
assign("family", "SAR", envir=env)
spam_setup(env)
get("similar", envir=env)
do_ldet(0.5, env)
rm(env)
env <- new.env(parent=globalenv())
assign("listw", lw, envir=env)
assign("n", length(boston.soi), envir=env)
assign("similar", FALSE, envir=env)
assign("family", "SAR", envir=env)
LU_setup(env)
get("similar", envir=env)
do_ldet(0.5, env)
rm(env)
env <- new.env(parent=globalenv())
assign("listw", lw, envir=env)
assign("n", length(boston.soi), envir=env)
assign("similar", FALSE, envir=env)
assign("family", "SAR", envir=env)
LU_prepermutate_setup(env)
get("similar", envir=env)
do_ldet(0.5, env)
rm(env)
env <- new.env(parent=globalenv())
assign("listw", lw, envir=env)
assign("similar", FALSE, envir=env)
assign("family", "SAR", envir=env)
cheb_setup(env, q=5)
get("similar", envir=env)
do_ldet(0.5, env)
rm(env)
env <- new.env(parent=globalenv())
assign("listw", lw, envir=env)
assign("n", length(boston.soi), envir=env)
assign("similar", FALSE, envir=env)
assign("family", "SAR", envir=env)
set.seed(12345)
mcdet_setup(env, p=16, m=30)
get("similar", envir=env)
do_ldet(0.5, env)
rm(env)

```

Description

An implementation of Kelejian and Prucha's generalised moments estimator for the autoregressive parameter in a spatial model.

Usage

```
GMerrorsar(formula, data = list(), listw, na.action = na.fail,
  zero.policy = attr(listw, "zero.policy"), method="nlminb", arnoldWied=FALSE,
  control = list(), pars, scaleU=FALSE, verbose=NULL, legacy=FALSE,
  se.lambda=TRUE, returnHcov=FALSE, pWOrder=250, tol.Hcov=1.0e-10)
## S3 method for class 'Gmsar'
summary(object, correlation = FALSE, Hausman=FALSE, ...)
GMargminImage(obj, lambdaseq, s2seq)
```

Arguments

formula	a symbolic description of the model to be fit. The details of model specification are given for <code>lm()</code>
data	an optional data frame containing the variables in the model. By default the variables are taken from the environment which the function is called.
listw	a <code>listw</code> object created for example by <code>nb2listw</code>
na.action	a function (default <code>na.fail</code>), can also be <code>na.omit</code> or <code>na.exclude</code> with consequences for residuals and fitted values - in these cases the weights list will be subsetted to remove NAs in the data. It may be necessary to set <code>zero.policy</code> to <code>TRUE</code> because this subsetting may create no-neighbour observations. Note that only weights lists created without using the <code>glist</code> argument to <code>nb2listw</code> may be subsetted.
zero.policy	default <code>NULL</code> , use global option value; if <code>TRUE</code> assign zero to the lagged value of zones without neighbours, if <code>FALSE</code> (default) assign <code>NA</code> - causing <code>GMerrorsar()</code> to terminate with an error
method	default <code>"nlminb"</code> , or optionally a method passed to <code>optim</code> to use an alternative optimizer
arnoldWied	default <code>FALSE</code>
control	A list of control parameters. See details in optim or nlminb .
pars	starting values for λ and σ^2 for GMM optimisation, if missing (default), approximated from initial OLS model as the autocorrelation coefficient corrected for weights style and model sigma squared
scaleU	Default <code>FALSE</code> : scale the OLS residuals before computing the moment matrices; only used if the <code>pars</code> argument is missing
verbose	default <code>NULL</code> , use global option value; if <code>TRUE</code> , reports function values during optimization.
legacy	default <code>FALSE</code> - compute using the unfiltered values of the response and right hand side variables; if <code>TRUE</code> - compute the fitted value and residuals from the spatially filtered model using the spatial error parameter

se.lambda	default TRUE, use the analytical method described in http://econweb.umd.edu/~prucha/STATPROG/OLS/deso1s.pdf
returnHcov	default FALSE, return the Vo matrix for a spatial Hausman test
tol.Hcov	the tolerance for computing the Vo matrix (default=1.0e-10)
pWOrder	default 250, if returnHcov=TRUE, pass this order to powerWeights as the power series maximum limit
object, obj	Gmsar object from GMerrorsar
correlation	logical; (default=FALSE), TRUE not available
Hausman	if TRUE, the results of the Hausman test for error models are reported
...	summary arguments passed through
lambdaseq	if given, an increasing sequence of lambda values for gridding
s2seq	if given, an increasing sequence of sigma squared values for gridding

Details

When the control list is set with care, the function will converge to values close to the ML estimator without requiring computation of the Jacobian, the most resource-intensive part of ML estimation.

Note that the fitted() function for the output object assumes that the response variable may be reconstructed as the sum of the trend, the signal, and the noise (residuals). Since the values of the response variable are known, their spatial lags are used to calculate signal components (Cressie 1993, p. 564). This differs from other software, including GeoDa, which does not use knowledge of the response variable in making predictions for the fitting data.

The GMargminImage may be used to visualize the shape of the surface of the argmin function used to find lambda.

Value

A list object of class Gmsar

type	"ERROR"
lambda	simultaneous autoregressive error coefficient
coefficients	GMM coefficient estimates
rest.se	GMM coefficient standard errors
s2	GMM residual variance
SSE	sum of squared GMM errors
parameters	number of parameters estimated
lm.model	the lm object returned when estimating for $\lambda = 0$
call	the call used to create this object
residuals	GMM residuals
lm.target	the lm object returned for the GMM fit
fitted.values	Difference between residuals and response variable
formula	model formula

aliased	if not NULL, details of aliased variables
zero.policy	zero.policy for this model
vv	list of internal bigG and litg components for testing optimisation surface
optres	object returned by optimizer
pars	start parameter values for optimisation
Hcov	Spatial DGP covariance matrix for Hausman test if available
legacy	input choice of unfiltered or filtered values
lambda.se	value computed if input argument TRUE
arnoldWied	were Arnold-Wied moments used
GMS2	GM argmin sigma squared
scaleU	input choice of scaled OLS residuals
vcov	variance-covariance matrix of regression coefficients
na.action	(possibly) named vector of excluded or omitted observations if non-default na.action argument used

Author(s)

Luc Anselin and Roger Bivand

References

Kelejian, H. H., and Prucha, I. R., 1999. A Generalized Moments Estimator for the Autoregressive Parameter in a Spatial Model. *International Economic Review*, 40, pp. 509–533; Cressie, N. A. C. 1993 *Statistics for spatial data*, Wiley, New York.

Roger Bivand, Gianfranco Piras (2015). Comparing Implementations of Estimation Methods for Spatial Econometrics. *Journal of Statistical Software*, 63(18), 1-36. [doi:10.18637/jss.v063.i18](https://doi.org/10.18637/jss.v063.i18).

See Also

[optim](#), [nlminb](#), [errorsarlm](#)

Examples

```
#require("spdep", quietly=TRUE)
data(oldcol, package="spdep")
COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  spdep::nb2listw(COL.nb, style="W"), method="eigen")
(x <- summary(COL.errW.eig, Hausman=TRUE))
coef(x)
COL.errW.GM <- GMerrorsar(CRIME ~ INC + HOVAL, data=COL.OLD,
  spdep::nb2listw(COL.nb, style="W"), returnHcov=TRUE)
(x <- summary(COL.errW.GM, Hausman=TRUE))
coef(x)
aa <- GMargminImage(COL.errW.GM)
levs <- quantile(aa$z, seq(0, 1, 1/12))
image(aa, breaks=levs, xlab="lambda", ylab="s2")
```

```

points(COL.errW.GM$lambda, COL.errW.GM$s2, pch=3, lwd=2)
contour(aa, levels=signif(levs, 4), add=TRUE)
COL.errW.GM1 <- GMerrorsar(CRIME ~ INC + HOVAL, data=COL.OLD,
  spdep::nb2listw(COL.nb, style="W"))
summary(COL.errW.GM1)
require("sf", quietly=TRUE)
nydata <- st_read(system.file("shapes/NY8_bna_utm18.gpkg", package="spData")[1], quiet=TRUE)
suppressMessages(nyadjmat <- as.matrix(foreign::read.dbf(system.file(
  "misc/nyadjwts.dbf", package="spData")[1])[-1]))
suppressMessages(ID <- as.character(names(foreign::read.dbf(system.file(
  "misc/nyadjwts.dbf", package="spData")[1])[-1]))
identical(substring(ID, 2, 10), substring(as.character(nydata$AREAKEY), 2, 10))
listw_NY <- spdep::mat2listw(nyadjmat, as.character(nydata$AREAKEY), style="B")
esar1f <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, family="SAR", method="eigen")
summary(esar1f)
esar1gm <- GMerrorsar(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME,
  data=nydata, listw=listw_NY)
summary(esar1gm)
esar1gm1 <- GMerrorsar(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME,
  data=nydata, listw=listw_NY, method="Nelder-Mead")
summary(esar1gm1)

```

griffith_sone

Spatial weights matrix eigenvalues

Description

The `eigenw` function returns a numeric vector of eigenvalues of the weights matrix generated from the spatial weights object `listw`. The eigenvalues are used to speed the computation of the Jacobian in spatial model estimation:

$$\log(\det[I - \rho W]) = \sum_{i=1}^n \log(1 - \rho \lambda_i)$$

where W is the n by n spatial weights matrix, and λ_i are the eigenvalues of W .

Usage

```

eigenw(listw, quiet=NULL)
griffith_sone(P, Q, type="rook")
subgraph_eigenw(nb, glist=NULL, style="W", zero.policy=NULL, quiet=NULL)

```

Arguments

<code>listw</code>	a <code>listw</code> object created for example by <code>nb2listw</code>
<code>quiet</code>	default <code>NULL</code> , use global <code>!verbose</code> option value; set to <code>FALSE</code> for short summary

P	number of columns in the grid (number of units in a horizontal axis direction)
Q	number of rows in the grid (number of units in a vertical axis direction.)
type	“rook” or “queen”
nb	an object of class nb
glist	list of general weights corresponding to neighbours
style	style can take values “W”, “B”, “C”, “U”, “minmax” and “S”
zero.policy	default NULL, use global option value; if FALSE stop with error for any empty neighbour sets, if TRUE permit the weights list to be formed with zero-length weights vectors

Details

The `griffith_sone` function may be used, following Ord and Gasim (for references see Griffith and Sone (1995)), to calculate analytical eigenvalues for binary rook or queen contiguous neighbours where the data are arranged as a regular P times Q grid. The `subgraph_eigenw` function may be used when there are multiple graph components, of which the largest may be handled as a dense matrix. Here the eigenvalues are computed for each subgraph in turn, and catenated to reconstruct the complete set. The functions may be used to provide pre-computed eigenvalues for spatial regression functions.

Value

a numeric or complex vector of eigenvalues of the weights matrix generated from the spatial weights object.

Author(s)

Roger Bivand <Roger.Bivand@nhh.no>

References

Cliff, A. D., Ord, J. K. 1981 Spatial processes, Pion, p. 155; Ord, J. K. 1975 Estimation methods for models of spatial interaction, Journal of the American Statistical Association, 70, 120-126.; Griffith, D. A. and Sone, A. (1995). Trade-offs associated with normalizing constant computational simplifications for estimating spatial statistical models. Journal of Statistical Computation and Simulation, 51, 165-183.

See Also

[eigen](#)

Examples

```
#require(spdep)
data(oldcol, package="spdep")
W.eig <- eigenw(spdep::nb2listw(COL.nb, style="W"))
1/range(W.eig)
S.eig <- eigenw(spdep::nb2listw(COL.nb, style="S"))
```

```

1/range(S.eig)
B.eig <- eigenw(spdep::nb2listw(COL.nb, style="B"))
1/range(B.eig)
# cases for intrinsically asymmetric weights
crds <- cbind(COL.OLD$X, COL.OLD$Y)
k3 <- spdep::knn2nb(spdep::knearneigh(crds, k=3))
spdep::is.symmetric.nb(k3)
k3eig <- eigenw(spdep::nb2listw(k3, style="W"))
is.complex(k3eig)
rho <- 0.5
Jc <- sum(log(1 - rho * k3eig))
# complex eigenvalue Jacobian
Jc
# subgraphs
nc <- attr(k3, "ncomp")
if (is.null(nc)) nc <- spdep::n.comp.nb(k3)
nc$nc
table(nc$comp.id)
k3eigSG <- subgraph_eigenw(k3, style="W")
all.equal(sort(k3eig), k3eigSG)
W <- as(spdep::nb2listw(k3, style="W"), "CsparseMatrix")
I <- diag(length(k3))
Jl <- sum(log(abs(diag(slot(lu(I - rho * W), "U")))))
# LU Jacobian equals complex eigenvalue Jacobian
Jl
all.equal(Re(Jc), Jl)
# wrong value if only real part used
Jr <- sum(log(1 - rho * Re(k3eig)))
Jr
all.equal(Jr, Jl)
# construction of Jacobian from complex conjugate pairs (Jan Hauke)
Rev <- Re(k3eig)[which(Im(k3eig) == 0)]
# real eigenvalues
Cev <- k3eig[which(Im(k3eig) != 0)]
pCev <- Cev[Im(Cev) > 0]
# separate complex conjugate pairs
RpCev <- Re(pCev)
IpCev <- Im(pCev)
# reassemble Jacobian
Jc1 <- sum(log(1 - rho*Rev)) + sum(log((1 - rho * RpCev)^2 + (rho^2)*(IpCev^2)))
all.equal(Re(Jc), Jc1)
# impact of omitted complex part term in real part only Jacobian
Jc2 <- sum(log(1 - rho*Rev)) + sum(log((1 - rho * RpCev)^2))
all.equal(Jr, Jc2)
# trace of asymmetric (WW) and crossprod of complex eigenvalues for APLE
sum(diag(W %*% W))
crossprod(k3eig)
# analytical regular grid eigenvalues
rg <- spdep::cell2nb(ncol=7, nrow=7, type="rook")
rg_eig <- eigenw(spdep::nb2listw(rg, style="B"))
rg_GS <- griffith_sone(P=7, Q=7, type="rook")
all.equal(rg_eig, rg_GS)
## Not run:

```

```

run <- FALSE
if (require("RSpectra", quietly=TRUE)) run <- TRUE
if (run) {
B <- as(spdep::nb2listw(rg, style="B"), "CsparseMatrix")
res1 <- eigs(B, k=1, which="LR")$values
resn <- eigs(B, k=1, which="SR")$values
print(Re(c(resn, res1)))
}
if (run) {
print(all.equal(range(Re(rg_eig)), c(resn, res1)))
}
if (run) {
lw <- spdep::nb2listw(rg, style="W")
rg_eig <- eigenw(similar.listw(lw))
print(range(Re(rg_eig)))
}
if (run) {
W <- as(lw, "CsparseMatrix")
print(Re(c(eigs(W, k=1, which="SR")$values, eigs(W, k=1, which="LR")$values)))
}
## End(Not run)

```

gstsls

*Spatial simultaneous autoregressive SAC model estimation by GMM***Description**

An implementation of Kelejian and Prucha's generalised moments estimator for the autoregressive parameter in a spatial model with a spatially lagged dependent variable.

Usage

```

gstsls(formula, data = list(), listw, listw2 = NULL, na.action = na.fail,
       zero.policy = attr(listw, "zero.policy"), pars=NULL, scaleU=FALSE, control = list(),
       verbose=NULL, method="nlminb", robust=FALSE, legacy=FALSE, W2X=TRUE, sig2n_k=FALSE)
## S3 method for class 'Gmsar'
impacts(obj, ..., n = NULL, tr = NULL, R = NULL,
       listw = NULL, evalues=NULL, tol = 1e-06, empirical = FALSE, Q=NULL)

```

Arguments

formula	a symbolic description of the model to be fit. The details of model specification are given for <code>lm()</code>
data	an optional data frame containing the variables in the model. By default the variables are taken from the environment which the function is called.
listw	a <code>listw</code> object created for example by <code>nb2listw</code>
listw2	a <code>listw</code> object created for example by <code>nb2listw</code> , if not given, set to the same spatial weights as the <code>listw</code> argument

na.action	a function (default <code>na.fail</code>), can also be <code>na.omit</code> or <code>na.exclude</code> with consequences for residuals and fitted values - in these cases the weights list will be subsetted to remove NAs in the data. It may be necessary to set <code>zero.policy</code> to <code>TRUE</code> because this subsetting may create no-neighbour observations. Note that only weights lists created without using the <code>glist</code> argument to <code>nb2listw</code> may be subsetted.
zero.policy	default <code>NULL</code> , use global option value; if <code>TRUE</code> assign zero to the lagged value of zones without neighbours, if <code>FALSE</code> (default) assign <code>NA</code> - causing <code>GMerrorsar()</code> to terminate with an error
pars	starting values for λ and σ^2 for GMM optimisation, if missing (default), approximated from initial 2sls model as the autocorrelation coefficient corrected for weights style and model sigma squared
scaleU	Default <code>FALSE</code> : scale the OLS residuals before computing the moment matrices; only used if the <code>pars</code> argument is missing
control	A list of control parameters. See details in optim or nlminb
verbose	default <code>NULL</code> , use global option value; if <code>TRUE</code> , reports function values during optimization.
method	default nlminb , or optionally a method passed to optim to use an alternative optimizer
robust	see <code>stsls</code>
legacy	see <code>stsls</code>
W2X	see <code>stsls</code>
sig2n_k	see <code>stsls</code>
obj	A spatial regression object created by <code>lagsarlm</code> , <code>lagmess</code> or by <code>lmSLX</code> ; in <code>HPDinterval.LagImpact</code> , a <code>LagImpact</code> object
...	Arguments passed through to methods in the cod a package
tr	A vector of traces of powers of the spatial weights matrix created using <code>trW</code> , for approximate impact measures; if not given, <code>listw</code> must be given for exact measures (for small to moderate spatial weights matrices); the traces must be for the same spatial weights as were used in fitting the spatial regression, and must be row-standardised
evalues	vector of eigenvalues of spatial weights matrix for impacts calculations
R	If given, simulations are used to compute distributions for the impact measures, returned as <code>mcmc</code> objects; the objects are used for convenience but are not output by an MCMC process
tol	Argument passed to <code>mvrnorm</code> : tolerance (relative to largest variance) for numerical lack of positive-definiteness in the coefficient covariance matrix
empirical	Argument passed to <code>mvrnorm</code> (default <code>FALSE</code>): if true, the coefficients and their covariance matrix specify the empirical not population mean and covariance matrix
Q	default <code>NULL</code> , else an integer number of cumulative power series impacts to calculate if <code>tr</code> is given
n	defaults to <code>length(obj\$residuals)</code> ; in the method for <code>Gmsar</code> objects it may be used in panel settings to compute the impacts for cross-sectional weights only, suggested by Angela Parenti

Details

When the control list is set with care, the function will converge to values close to the ML estimator without requiring computation of the Jacobian, the most resource-intensive part of ML estimation.

Value

A list object of class Gmsar

lambda	simultaneous autoregressive error coefficient
coefficients	GMM coefficient estimates (including the spatial autocorrelation coefficient)
rest.se	GMM coefficient standard errors
s2	GMM residual variance
SSE	sum of squared GMM errors
parameters	number of parameters estimated
lm.model	NULL
call	the call used to create this object
residuals	GMM residuals
lm.target	NULL
fitted.values	Difference between residuals and response variable
formula	model formula
aliased	NULL
zero.policy	zero.policy for this model
LL	NULL
vv	list of internal bigG and litg components for testing optimisation surface
optres	object returned by optimizer
pars	start parameter values for optimisation
Hcov	NULL
na.action	(possibly) named vector of excluded or omitted observations if non-default na.action argument used

Author(s)

Gianfranco Piras and Roger Bivand

References

- Kelejian, H. H., and Prucha, I. R., 1999. A Generalized Moments Estimator for the Autoregressive Parameter in a Spatial Model. *International Economic Review*, 40, pp. 509–533; Cressie, N. A. C. 1993 *Statistics for spatial data*, Wiley, New York.
- Roger Bivand, Gianfranco Piras (2015). Comparing Implementations of Estimation Methods for Spatial Econometrics. *Journal of Statistical Software*, 63(18), 1-36. doi:10.18637/jss.v063.i18.

See Also

[optim](#), [nlminb](#), [GMerrorsar](#), [GMargminImage](#)

Examples

```
#require("spdep", quietly=TRUE)
data(oldcol, package="spdep")
COL.errW.GM <- gsts1s(CRIME ~ INC + HOVAL, data=COL.OLD, spdep::nb2listw(COL.nb, style="W"))
summary(COL.errW.GM)
aa <- GMargminImage(COL.errW.GM)
levs <- quantile(aa$z, seq(0, 1, 1/12))
image(aa, breaks=levs, xlab="lambda", ylab="s2")
points(COL.errW.GM$lambda, COL.errW.GM$s2, pch=3, lwd=2)
contour(aa, levels=signif(levs, 4), add=TRUE)
COL.errW.GM <- gsts1s(CRIME ~ INC + HOVAL, data=COL.OLD,
  spdep::nb2listw(COL.nb, style="W"), scaleU=TRUE)
summary(COL.errW.GM)
listw <- spdep::nb2listw(COL.nb)
W <- as(listw, "CsparseMatrix")
trMat <- trW(W, type="mult")
impacts(COL.errW.GM, tr=trMat)
```

impacts

Impacts in spatial lag models

Description

The calculation of impacts for spatial lag and spatial Durbin models is needed in order to interpret the regression coefficients correctly, because of the spillovers between the terms in these data generation processes (unlike the spatial error model). Methods for “SLX” and Bayesian fitted models are also provided, the former do not need MC simulations, while the latter pass through MCMC draws.

Usage

```
#\method{impacts}{sarlm}(obj, \dots, tr, R = NULL, listw = NULL, evalues=NULL,
# useHESS = NULL, tol = 1e-06, empirical = FALSE, Q=NULL)
#\method{impacts}{lagmess}(obj, ..., R=NULL, listw=NULL, tol=1e-6,
# empirical=FALSE)
#\method{impacts}{SLX}(obj, ...)
#\method{impacts}{MCMC_sar_g}(obj, ..., tr=NULL, listw=NULL, evalues=NULL, Q=NULL)
#\method{impacts}{MCMC_sem_g}(obj, ..., tr=NULL, listw=NULL, evalues=NULL, Q=NULL)
#\method{impacts}{MCMC_sac_g}(obj, ..., tr=NULL, listw=NULL, evalues=NULL, Q=NULL)
## S3 method for class 'LagImpact'
plot(x, ..., choice="direct", trace=FALSE, density=TRUE)
## S3 method for class 'LagImpact'
print(x, ..., reportQ=NULL)
## S3 method for class 'LagImpact'
```

```
summary(object, ..., zstats=FALSE, short=FALSE, reportQ=NULL)
#\method{print}{WXImpact}(x, ...)
#\method{summary}{WXImpact}(object, ..., adjust_k=(attr(object, "type") == "SDEM"))
## S3 method for class 'LagImpact'
HPDinterval(obj, prob = 0.95, ..., choice="direct")
intImpacts(rho, beta, P, n, mu, Sigma, irho, drop2beta, bnames, interval,
  type, tr, R, listw, evalues, tol, empirical, Q, icept, iicept, p, mess=FALSE,
  samples=NULL, zero_fill = NULL, dvars = NULL)
```

Arguments

obj	A spatial regression object created by <code>lagsarlm</code> or by <code>lmSLX</code> ; in <code>HPDinterval.LagImpact</code> , a <code>LagImpact</code> object
...	Arguments passed through to methods in the <code>coda</code> package
tr	A vector of traces of powers of the spatial weights matrix created using <code>trW</code> , for approximate impact measures; if not given, <code>listw</code> must be given for exact measures (for small to moderate spatial weights matrices); the traces must be for the same spatial weights as were used in fitting the spatial regression, and must be row-standardised
listw	If <code>tr</code> is not given, a spatial weights object as created by <code>nb2listw</code> ; they must be the same spatial weights as were used in fitting the spatial regression, but do not have to be row-standardised
evalues	vector of eigenvalues of spatial weights matrix for impacts calculations
n	defaults to <code>length(obj\$residuals)</code> ; in the method for <code>gmsar</code> objects it may be used in panel settings to compute the impacts for cross-sectional weights only, suggested by Angela Parenti
R	If given, simulations are used to compute distributions for the impact measures, returned as <code>mcmc</code> objects; the objects are used for convenience but are not output by an MCMC process
useHESS	Use the Hessian approximation (if available) even if the asymptotic coefficient covariance matrix is available; used for comparing methods
tol	Argument passed to <code>mvrnorm</code> : tolerance (relative to largest variance) for numerical lack of positive-definiteness in the coefficient covariance matrix
empirical	Argument passed to <code>mvrnorm</code> (default <code>FALSE</code>): if true, the coefficients and their covariance matrix specify the empirical not population mean and covariance matrix
Q	default <code>NULL</code> , else an integer number of cumulative power series impacts to calculate if <code>tr</code> is given
reportQ	default <code>NULL</code> ; if <code>TRUE</code> and <code>Q</code> given as an argument to <code>impacts</code> , report impact components
x, object	<code>LagImpact</code> objects created by <code>impacts</code> methods
zstats	default <code>FALSE</code> , if <code>TRUE</code> , also return z-values and p-values for the impacts based on the simulations
short	default <code>FALSE</code> , if <code>TRUE</code> passed to the print summary method to omit printing of the <code>mcmc</code> summaries

choice	One of three impacts: direct, indirect, or total
trace	Argument passed to <code>plot.mcmc</code> : plot trace plots
density	Argument passed to <code>plot.mcmc</code> : plot density plots
prob	Argument passed to <code>HPDinterval.mcmc</code> : a numeric scalar in the interval (0,1) giving the target probability content of the intervals
adjust_k	default TRUE if SDEM else FALSE, adjust internal OLS SDEM standard errors by dividing by n rather than (n-k) (default changed and bug fixed after 0.7-8; standard errors now ML in SDEM summary and impacts summary and identical - for SLX use FALSE)
rho, beta, P, mu, Sigma, irho, drop2beta, bnames, interval, type, icept, iicept, p, mess, samples, zero_fill, dvars	internal arguments shared inside impacts methods

Details

If called without `R` being set, the method returns the direct, indirect and total impacts for the variables in the model, for the variables themselves in the spatial lag model case, for the variables and their spatial lags in the spatial Durbin (mixed) model case. The spatial lag impact measures are computed using eq. 2.46 (LeSage and Pace, 2009, p. 38), either using the exact dense matrix (when `listw` is given), or traces of powers of the weights matrix (when `tr` is given). When the traces are created by powering sparse matrices, the exact and the trace methods should give very similar results, unless the number of powers used is very small, or the spatial coefficient is close to its bounds.

If `R` is given, simulations will be used to create distributions for the impact measures, provided that the fitted model object contains a coefficient covariance matrix. The simulations are made using `mvrnorm` with the coefficients and their covariance matrix from the fitted model.

The simulations are stored as `mcmc` objects as defined in the `coda` package; the objects are used for convenience but are not output by an MCMC process. The simulated values of the coefficients are checked to see that the spatial coefficient remains within its valid interval — draws outside the interval are discarded.

If a model is fitted with the “Durbin=” set to a formula subsetting the explanatory variables, the impacts object returned reports Durbin impacts for variables included in the formula and lag impacts for the other variables.

When `Q` and `tr` are given, addition impact component results are provided for each step in the traces of powers of the weights matrix up to and including the Q 'th power. This increases computing time because the output object is substantially increased in size in proportion to the size of Q .

The method for `gmsar` objects is only for those of type SARAR output by `gsts1s`, and assume that the spatial error coefficient is fixed, and thus omitted from the coefficients and covariance matrix used for simulation.

Value

An object of class `LagImpact`.

If no simulation is carried out, the object returned is a list with:

`direct` numeric vector

indirect numeric vector
total numeric vector

and a matching Qres list attribute if Q was given.

If simulation is carried out, the object returned is a list with:

res a list with three components as for the non-simulation case, with a matching Qres list attribute if Q was given
sres a list with three mcmc matrices, for the direct, indirect and total impacts with a matching Qmcmc list attribute if Q was given

Author(s)

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References

LeSage J and RK Pace (2009) *Introduction to Spatial Econometrics*. CRC Press, Boca Raton, pp. 33–42, 114–115; LeSage J and MM Fischer (2008) Spatial growth regressions: model specification, estimation and interpretation. *Spatial Economic Analysis* 3 (3), pp. 275–304.

Roger Bivand, Gianfranco Piras (2015). Comparing Implementations of Estimation Methods for Spatial Econometrics. *Journal of Statistical Software*, 63(18), 1-36. doi:10.18637/jss.v063.i18.

See Also

[trW](#), [lagsarlm](#), [nb2listw](#), [mvrnorm](#), [plot.mcmc](#), [summary.mcmc](#), [HPDinterval](#)

Examples

```
require("sf", quietly=TRUE)
columbus <- st_read(system.file("shapes/columbus.gpkg", package="spData")[1], quiet=TRUE)
#require("spdep", quietly=TRUE)
col.gal.nb <- spdep::read.gal(system.file("weights/columbus.gal", package="spData")[1])
listw <- spdep::nb2listw(col.gal.nb)
ev <- eigenw(listw)
lobj <- lagsarlm(CRIME ~ INC + HOVAL, columbus, listw,
  control=list(pre_eig=ev))
summary(lobj)
mobj <- lagsarlm(CRIME ~ INC + HOVAL, columbus, listw, Durbin=TRUE,
  control=list(pre_eig=ev))
summary(mobj)
mobj1 <- lagsarlm(CRIME ~ INC + HOVAL, columbus, listw, Durbin= ~ INC,
  control=list(pre_eig=ev))
summary(mobj1)
W <- as(listw, "CsparseMatrix")
trMatc <- trW(W, type="mult")
trMC <- trW(W, type="MC")
set.seed(1)
impacts(lobj, listw=listw)
impacts(lobj, tr=trMatc)
```

```

impacts(lobj, tr=trMC)
impacts(lobj, evalues=ev)
library(coda)
lobjIQ5 <- impacts(lobj, tr=trMatc, R=200, Q=5)
summary(lobjIQ5, zstats=TRUE, short=TRUE)
summary(lobjIQ5, zstats=TRUE, short=TRUE, reportQ=TRUE)
impacts(mobj, listw=listw)
impacts(mobj, tr=trMatc)
impacts(mobj, tr=trMC)
impacts(mobj1, tr=trMatc)
impacts(mobj1, listw=listw)
## Not run:
try(impacts(mobj, evalues=ev), silent=TRUE)

## End(Not run)
summary(impacts(mobj, tr=trMatc, R=200), short=TRUE, zstats=TRUE)
summary(impacts(mobj1, tr=trMatc, R=200), short=TRUE, zstats=TRUE)
xobj <- lmSLX(CRIME ~ INC + HOVAL, columbus, listw)
summary(impacts(xobj))
eobj <- errorsarlm(CRIME ~ INC + HOVAL, columbus, listw, etype="emixed")
summary(impacts(eobj), adjust_k=TRUE)
## Not run:
mobj1 <- lagsarlm(CRIME ~ INC + HOVAL, columbus, listw, type="mixed",
method="Matrix", control=list(fdHess=TRUE))
summary(mobj1)
set.seed(1)
summary(impacts(mobj1, tr=trMatc, R=1000), zstats=TRUE, short=TRUE)
summary(impacts(mobj, tr=trMatc, R=1000), zstats=TRUE, short=TRUE)
mobj2 <- lagsarlm(CRIME ~ INC + HOVAL, columbus, listw, type="mixed",
method="Matrix", control=list(fdHess=TRUE, optimHess=TRUE))
summary(impacts(mobj2, tr=trMatc, R=1000), zstats=TRUE, short=TRUE)
mobj3 <- lagsarlm(CRIME ~ INC + HOVAL, columbus, listw, type="mixed",
method="spam", control=list(fdHess=TRUE))
summary(impacts(mobj3, tr=trMatc, R=1000), zstats=TRUE, short=TRUE)

## End(Not run)
## Not run:
data(boston, package="spData")
Wb <- as(spdep::nb2listw(boston.soi), "CsparseMatrix")
trMatb <- trW(Wb, type="mult")
gp2mMi <- lagsarlm(log(CMEDV) ~ CRIM + ZN + INDUS + CHAS + I(NOX^2) +
I(RM^2) + AGE + log(DIS) + log(RAD) + TAX + PTRATIO + B + log(LSTAT),
data=boston.c, spdep::nb2listw(boston.soi), type="mixed", method="Matrix",
control=list(fdHess=TRUE), trs=trMatb)
summary(gp2mMi)
summary(impacts(gp2mMi, tr=trMatb, R=1000), zstats=TRUE, short=TRUE)
#data(house, package="spData")
#lw <- spdep::nb2listw(L0_nb)
#form <- formula(log(price) ~ age + I(age^2) + I(age^3) + log(lotsize) +
# rooms + log(TLA) + beds + syeur)
#lobj <- lagsarlm(form, house, lw, method="Matrix",
# control=list(fdHess=TRUE), trs=trMat)
#summary(lobj)

```

```

#loobj <- impacts(loobj, tr=trMat, R=1000)
#summary(loobj, zstats=TRUE, short=TRUE)
#loobj1 <- stsls(form, house, lw)
#loobj1 <- impacts(loobj1, tr=trMat, R=1000)
#summary(loobj1, zstats=TRUE, short=TRUE)
#mobj <- lagsarlm(form, house, lw, type="mixed",
# method="Matrix", control=list(fdHess=TRUE), trs=trMat)
#summary(mobj)
#moobj <- impacts(mobj, tr=trMat, R=1000)
#summary(moobj, zstats=TRUE, short=TRUE)

## End(Not run)

```

invIrM

Compute SAR generating operator

Description

Computes the matrix used for generating simultaneous autoregressive random variables, for a given value of rho, a neighbours list object or a matrix, a chosen coding scheme style, and optionally a list of general weights corresponding to neighbours.

Usage

```

invIrM(neighbours, rho, glist=NULL, style="W", method="solve",
feasible=NULL)
invIrW(x, rho, method="solve", feasible=NULL)

```

Arguments

neighbours	an object of class nb
rho	autoregressive parameter
glist	list of general weights corresponding to neighbours
style	style can take values W, B, C, and S
method	default solve, can also take value chol
feasible	if NULL, the given value of rho is checked to see if it lies within its feasible range, if TRUE, the test is not conducted
x	either a listw object from for example nb2listw or a square spatial weights matrix, optionally a sparse matrix

Details

The invIrW function generates the full weights matrix V, checks that rho lies in its feasible range between $1/\min(\text{eigen}(V))$ and $1/\max(\text{eigen}(V))$, and returns the nxn inverted matrix

$$(I - \rho V)^{-1}$$

. With method="chol" (only for a listw object), Cholesky decomposition is used, thanks to contributed code by Markus Reeder and Werner Mueller.

Note that, in some situations in simulation, it may matter that the random vector from `rnorm` or similar will not be exactly $N(0, 1)$, and it will also contain random amounts of spatial autocorrelation itself, which will mix with the spatial autocorrelation injected by the process operator

$$(I - \rho V)^{-1}$$

. In addition, it will not follow the stipulated distribution exactly either, so that several steps may be needed to scale the random vector, to remove artefacts coming from its deviance from distributional parameters, and to remove random spatial autocorrelation - see the examples below. Thanks to Rune Østergaard Pedersen for bring up this question.

The `powerWeights` function uses power series summation to cumulate the product

$$(I - \rho V)^{-1} \% * \% X$$

from

$$(I + \rho V + (\rho V)^2 + \dots) \% * \% X$$

, which can be done by storing only sparse V and several matrices of the same dimensions as X . This makes it possible to handle larger spatial weights matrices, but is sensitive to the power weights order and the tolerance arguments when the spatial coefficient is close to its bounds, leading to incorrect estimates of the implied inverse matrix.

Value

An $n \times n$ matrix with a "call" attribute; the `powerWeights` function returns a matrix of the same dimensions as X which has been multiplied by the power series equivalent of the dense matrix

$$(I - \rho V)^{-1}$$

.

Note

Before version 0.6-10, `powerWeights` only worked correctly for positive rho, with differences from true values increasing as rho approached -1, and exploding between -1 and the true negative bound.

Author(s)

Roger Bivand <Roger.Bivand@nhh.no>

References

Tiefelsdorf, M., Griffith, D. A., Boots, B. 1999 A variance-stabilizing coding scheme for spatial link matrices, *Environment and Planning A*, 31, pp. 165-180; Tiefelsdorf, M. 2000 Modelling spatial processes, *Lecture notes in earth sciences*, Springer, p. 76; Haining, R. 1990 *Spatial data analysis in the social and environmental sciences*, Cambridge University Press, p. 117; Cliff, A. D., Ord, J. K. 1981 *Spatial processes*, Pion, p. 152; Reeder, M. and Mueller, W. (2007) An Improvement of the `invIrM` Routine of the Geostatistical R-package `spdep` by Cholesky Inversion, *Statistical Projects*, LV No: 238.205, SS 2006, Department of Applied Statistics, Johannes Kepler University, Linz

See Also[nb2listw](#)**Examples**

```

library(spdep)
nb7rt <- cell2nb(7, 7, torus=TRUE)
lw <- nb2listw(nb7rt, style="W")
set.seed(1)
x <- matrix(sample(rnorm(500*length(nb7rt))), nrow=length(nb7rt))
if (requireNamespace("spatialreg", quietly=TRUE)) {
# Only needed in some simulation settings where the input and
# output distributions must agree in all but autocorrelation
if (FALSE) {
e <- spatialreg::eigenw(lw)
x <- apply(x, 2, scale)
st <- apply(x, 2, function(x) shapiro.test(x)$p.value)
x <- x[, (st > 0.2 & st < 0.8)]
x <- apply(x, 2, function(v) spatialreg::residuals.spautolm(
spatialreg::spautolm(v ~ 1, listw=lw, method="eigen",
control=list(pre_eig=e, fdHess=FALSE))))
x <- apply(x, 2, scale)
}
res0 <- apply(invIrM(nb7rt, rho=0.0, method="chol",
feasible=TRUE) %*% x, 2, function(x) var(x)/length(x))
res2 <- apply(invIrM(nb7rt, rho=0.2, method="chol",
feasible=TRUE) %*% x, 2, function(x) var(x)/length(x))
res4 <- apply(invIrM(nb7rt, rho=0.4, method="chol",
feasible=TRUE) %*% x, 2, function(x) var(x)/length(x))
res6 <- apply(invIrM(nb7rt, rho=0.6, method="chol",
feasible=TRUE) %*% x, 2, function(x) var(x)/length(x))
res8 <- apply(invIrM(nb7rt, rho=0.8, method="chol",
feasible=TRUE) %*% x, 2, function(x) var(x)/length(x))
res9 <- apply(invIrM(nb7rt, rho=0.9, method="chol",
feasible=TRUE) %*% x, 2, function(x) var(x)/length(x))
plot(density(res9), col="red", xlim=c(-0.01, max(density(res9)$x)),
ylim=range(density(res0)$y),
xlab="estimated variance of the mean",
main=expression(paste("Effects of spatial autocorrelation for different ",
rho, " values")))
lines(density(res0), col="black")
lines(density(res2), col="brown")
lines(density(res4), col="green")
lines(density(res6), col="orange")
lines(density(res8), col="pink")
legend(c(-0.02, 0.01), c(7, 25),
legend=c("0.0", "0.2", "0.4", "0.6", "0.8", "0.9"),
col=c("black", "brown", "green", "orange", "pink", "red"), lty=1, bty="n")
}
## Not run:
x <- matrix(rnorm(length(nb7rt)), ncol=1)
system.time(e <- invIrM(nb7rt, rho=0.9, method="chol", feasible=TRUE) %*% x)

```

```

system.time(e <- invIrM(nb7rt, rho=0.9, method="chol", feasible=NULL) %*% x)
system.time(e <- invIrM(nb7rt, rho=0.9, method="solve", feasible=TRUE) %*% x)
system.time(e <- invIrM(nb7rt, rho=0.9, method="solve", feasible=NULL) %*% x)

## End(Not run)

```

lagmess

Matrix exponential spatial lag model

Description

The function fits a matrix exponential spatial lag model, using `optim` to find the value of α , the spatial coefficient.

Usage

```

lagmess(formula, data = list(), listw, zero.policy = NULL, na.action = na.fail,
q = 10, start = -2.5, control=list(), method="BFGS", verbose=NULL,
use_expm=FALSE)

```

Arguments

<code>formula</code>	a symbolic description of the model to be fit. The details of model specification are given for <code>lm()</code>
<code>data</code>	an optional data frame containing the variables in the model. By default the variables are taken from the environment which the function is called.
<code>listw</code>	a <code>listw</code> object created for example by <code>spdep::nb2listw()</code>
<code>zero.policy</code>	default <code>NULL</code> , use global option value; if <code>TRUE</code> assign zero to the lagged value of zones without neighbours, if <code>FALSE</code> assign <code>NA</code> - causing <code>lagmess()</code> to terminate with an error
<code>na.action</code>	a function (default <code>options("na.action")</code>), can also be <code>na.omit</code> or <code>na.exclude</code> with consequences for residuals and fitted values - in these cases the weights list will be subsetted to remove <code>NA</code> s in the data. It may be necessary to set <code>zero.policy</code> to <code>TRUE</code> because this subsetting may create no-neighbour observations. Note that only weights lists created without using the <code>glist</code> argument to <code>nb2listw</code> may be subsetted.
<code>q</code>	default 10; number of powers of the spatial weights to use
<code>start</code>	starting value for numerical optimization, should be a small negative number
<code>control</code>	control parameters passed to <code>optim</code>
<code>method</code>	default <code>BFGS</code> , method passed to <code>optim</code>
<code>verbose</code>	default <code>NULL</code> , use global option value; if <code>TRUE</code> report function values during optimization
<code>use_expm</code>	default <code>FALSE</code> ; if <code>TRUE</code> use <code>expm::expAtv</code> instead of a truncated power series of W

Details

The underlying spatial lag model:

$$y = \rho W y + X \beta + \varepsilon$$

where ρ is the spatial parameter may be fitted by maximum likelihood. In that case, the log likelihood function includes the logarithm of cumbersome Jacobian term $|I - \rho W|$. If we rewrite the model as:

$$S y = X \beta + \varepsilon$$

we see that in the ML case $S y = (I - \rho W) y$. If W is row-stochastic, S may be expressed as a linear combination of row-stochastic matrices. By pre-computing the matrix $[y, W y, W^2 y, \dots, W^{q-1} y]$, the term $S y(\alpha)$ can readily be found by numerical optimization using the matrix exponential approach. α and ρ are related as $\rho = 1 - \exp \alpha$, conditional on the number of matrix power terms taken q .

Value

The function returns an object of class `Lagmess` with components:

<code>lmobj</code>	the <code>lm</code> object returned after fitting <code>alpha</code>
<code>alpha</code>	the spatial coefficient
<code>alphase</code>	the standard error of the spatial coefficient using the numerical Hessian
<code>rho</code>	the value of <code>rho</code> implied by <code>alpha</code>
<code>bestmess</code>	the object returned by <code>optim</code>
<code>q</code>	the number of powers of the spatial weights used
<code>start</code>	the starting value for numerical optimization used
<code>na.action</code>	(possibly) named vector of excluded or omitted observations if non-default <code>na.action</code> argument used
<code>nulllll</code>	the log likelihood of the aspatial model for the same data

Author(s)

Roger Bivand <Roger.Bivand@nhh.no> and Eric Blankmeyer

References

J. P. LeSage and R. K. Pace (2007) A matrix exponential specification. *Journal of Econometrics*, 140, 190-214; J. P. LeSage and R. K. Pace (2009) *Introduction to Spatial Econometrics*. CRC Press, Chapter 9.

See Also

[lagsarlm](#), [optim](#)

Examples

```
#require(spdep, quietly=TRUE)
data(baltimore, package="spData")
baltimore$AGE <- ifelse(baltimore$AGE < 1, 1, baltimore$AGE)
lw <- spdep::nb2listw(spdep::knn2nb(spdep::knearneigh(cbind(baltimore$X, baltimore$Y), k=7)))
obj1 <- lm(log(PRICE) ~ PATIO + log(AGE) + log(SQFT),
  data=baltimore)
spdep::lm.morantest(obj1, lw)
spdep::lm.LMtests(obj1, lw, test="all")
system.time(obj2 <- lagmess(log(PRICE) ~ PATIO + log(AGE) + log(SQFT), data=baltimore, listw=lw)
(x <- summary(obj2))
coef(x)
has_expm <- require("expm", quietly=TRUE)
if (has_expm) {
system.time(
obj2a <- lagmess(log(PRICE) ~ PATIO + log(AGE) + log(SQFT), data=baltimore, listw=lw, use_expm=TRUE)
)
summary(obj2a)
}
obj3 <- lagsarlm(log(PRICE) ~ PATIO + log(AGE) + log(SQFT), data=baltimore, listw=lw)
summary(obj3)

data(boston, package="spData")
lw <- spdep::nb2listw(boston.soi)
gp2 <- lagsarlm(log(CMEDV) ~ CRIM + ZN + INDUS + CHAS + I(NOX^2) + I(RM^2)
+ AGE + log(DIS) + log(RAD) + TAX + PTRATIO + B + log(LSTAT),
  data=boston.c, lw, method="Matrix")
summary(gp2)
gp2a <- lagmess(CMEDV ~ CRIM + ZN + INDUS + CHAS + I(NOX^2) + I(RM^2)
+ AGE + log(DIS) + log(RAD) + TAX + PTRATIO + B + log(LSTAT),
  data=boston.c, lw)
summary(gp2a)
```

lextrB

Find extreme eigenvalues of binary symmetric spatial weights

Description

The functions find extreme eigenvalues of binary symmetric spatial weights, when these form planar graphs; general weights are not permitted. `l_max` finds the largest eigenvalue using Rayleigh quotient methods of any “listw” object. `lextrB` first calls `l_max`, and uses its output to find the smallest eigenvalue in addition for binary symmetric spatial weights. `lextrW` extends these to find the smallest eigenvalue for intrinsically symmetric row-standardized binary weights matrices (transformed to symmetric through similarity internally). `lextrS` does the same for variance-stabilized (“S” style) intrinsically symmetric binary weights matrices (transformed to symmetric through similarity internally).

Usage

```
lextrB(lw, zero.policy = TRUE, control = list())
lextrW(lw, zero.policy=TRUE, control=list())
lextrS(lw, zero.policy=TRUE, control=list())
l_max(lw, zero.policy=TRUE, control=list())
```

Arguments

lw	a binary symmetric listw object from, for example, nb2listw with style “B” for lextrB, style “W” for lextrW and style “S” for lextrS; for l_max, the object may be asymmetric and does not have to be binary
zero.policy	default NULL, use global option value; if TRUE assign zero to the lagged value of zones without neighbours, if FALSE assign NA
control	a list of control arguments

Value

The functions return approximations to the extreme eigenvalues with the eigenvectors returned as attributes of this object.

Control arguments

trace report values in while loops, default NULL assuming FALSE; logical

tol tolerance for breaking while loops, default $.Machine$double.eps^{(1/2)}$; numeric

maxiter maximum number of iterations in while loops, default $6 * (\text{length}(lw\$neighbours) - 2)$; integer

useC use C code, default TRUE, logical (not in l_max)

Note

It may be necessary to modify control arguments if warnings about lack of convergence are seen.

Author(s)

Roger Bivand, Yongwan Chun, Daniel Griffith

References

Griffith, D. A. (2004). Extreme eigenfunctions of adjacency matrices for planar graphs employed in spatial analyses. *Linear Algebra and its Applications*, 388:201–219.

Examples

```
data(boston, package="spData")
#require(spdep, quietly=TRUE)
ab.listb <- spdep::nb2listw(boston.soi, style="B")
er <- range(eigenw(ab.listb))
er
```

```

res_1 <- lexB(ab.listb)
c(res_1)
run <- FALSE
if (require("RSpectra", quietly=TRUE)) run <- TRUE
if (run) {
  B <- as(ab.listb, "CsparseMatrix")
  eigs(B, k=1, which="SR")$values
}
if (run) {
  eigs(B, k=1, which="LR")$values
}
k5 <- spdep::knn2nb(spdep::knearneigh(boston.utm, k=5))
c(l_max(spdep::nb2listw(k5, style="B")))
max(Re(eigenw(spdep::nb2listw(k5, style="B"))))
c(l_max(spdep::nb2listw(k5, style="C")))
max(Re(eigenw(spdep::nb2listw(k5, style="C"))))
ab.listw <- spdep::nb2listw(boston.soi, style="W")
er <- range(eigenw(similar.listw(ab.listw)))
er
res_1 <- lextrW(ab.listw)
c(res_1)
if (run) {
  B <- as(similar.listw(ab.listw), "CsparseMatrix")
  eigs(B, k=1, which="SR")$values
}
if (run) {
  eigs(B, k=1, which="LR")$values
}
## Not run:
ab.listw <- spdep::nb2listw(boston.soi, style="S")
er <- range(eigenw(similar.listw(ab.listw)))
er
res_1 <- lextrS(ab.listw)
c(res_1)

## End(Not run)
if (run) {
  B <- as(similar.listw(ab.listw), "CsparseMatrix")
  eigs(B, k=1, which="SR")$values
}
if (run) {
  eigs(B, k=1, which="LR")$values
}

```

lmSLX

Spatial Durbin linear (SLX, spatially lagged X) model

Description

lmSLX fits an lm model augmented with the spatially lagged RHS variables, including the lagged

intercept when the spatial weights are not row-standardised. `create_WX` creates spatially lagged RHS variables, and is exposed for use in model fitting functions.

Usage

```
lmSLX(formula, data = list(), listw, na.action, weights=NULL, Durbin=TRUE,
       zero.policy=NULL, return_impacts=TRUE)
## S3 method for class 'SLX'
print(x, digits = max(3L, getOption("digits") - 3L), ...)
## S3 method for class 'SLX'
summary(object, correlation = FALSE, symbolic.cor = FALSE, ...)
## S3 method for class 'summary.SLX'
print(x, digits = max(3L, getOption("digits") - 3L),
      symbolic.cor = x$symbolic.cor, signif.stars = getOption("show.signif.stars"), ...)
## S3 method for class 'SLX'
impacts(obj, ...)
## S3 method for class 'WXimpact'
print(x, ...)
## S3 method for class 'WXimpact'
summary(object, ..., adjust_k=(attr(object, "type") == "SDEM"))
## S3 method for class 'SLX'
predict(object, newdata, listw, zero.policy=NULL, ...)
create_WX(x, listw, zero.policy=NULL, prefix="")
```

Arguments

<code>formula</code>	a symbolic description of the model to be fit. The details of model specification are given for <code>lm()</code>
<code>data</code>	an optional data frame containing the variables in the model. By default the variables are taken from the environment which the function is called.
<code>listw</code>	a <code>listw</code> object created for example by <code>nb2listw</code>
<code>na.action</code>	a function (default <code>options("na.action")</code>), can also be <code>na.omit</code> or <code>na.exclude</code> with consequences for residuals and fitted values - in these cases the spatial weights list will be subsetted to remove NAs in the data. It may be necessary to set <code>zero.policy</code> to <code>TRUE</code> because this subsetting may create no-neighbour observations. Note that only weights lists created without using the <code>glist</code> argument to <code>nb2listw</code> may be subsetted.
<code>weights</code>	an optional vector of weights to be used in the fitting process. Non-NULL weights can be used to indicate that different observations have different variances (with the values in weights being inversely proportional to the variances); or equivalently, when the elements of weights are positive integers w_i , that each response y_i is the mean of w_i unit-weight observations (including the case that there are w_i observations equal to y_i and the data have been summarized) - lm
<code>Durbin</code>	default <code>TRUE</code> for <code>lmSLX</code> (Durbin model including WX); if <code>TRUE</code> , full spatial Durbin model; if a formula object, the subset of explanatory variables to lag
<code>zero.policy</code>	default <code>NULL</code> , use global option value; if <code>TRUE</code> assign zero to the lagged value of zones without neighbours, if <code>FALSE</code> assign NA

return_impacts	default TRUE; may be set FALSE to avoid problems calculating impacts with aliased variables
digits	the number of significant digits to use when printing
correlation	logical; if TRUE, the correlation matrix of the estimated parameters is returned and printed
symbolic.cor	logical. If TRUE, print the correlations in a symbolic form (see 'symnum') rather than as numbers
signif.stars	logical. If TRUE, 'significance stars' are printed for each coefficient
obj	A spatial regression object created by lmSLX
...	Arguments passed through
prefix	default empty string, may be "lag" in some cases
x, object	model matrix to be lagged; lagImpact objects created by impacts methods
adjust_k	default TRUE if SDEM else FALSE, adjust internal OLS SDEM standard errors by dividing by n rather than (n-k) (default changed and bug fixed after 0.7-8; standard errors now ML in SDEM summary and impacts summary and identical - for SLX use FALSE)
newdata	data frame in which to predict — if NULL, predictions are for the data on which the model was fitted. Should have row names corresponding to region.id. If row names are exactly the same than the ones used for training, it uses in-sample predictors for forecast.

Value

The `lmSLX` function returns an "lm" object with a "mixedImps" list of three impact matrixes (impacts and standard errors) for direct, indirect and total impacts; total impacts calculated using a simplified local copy of the estimable function from the `gmodels` package.

Author(s)

Roger Bivand <Roger.Bivand@nhh.no>

See Also

[lm](#)

Examples

```
data(oldcol, package="spdep")
lw <- spdep::nb2listw(COL.nb, style="W")
COL.SLX <- lmSLX(CRIME ~ INC + HOVAL, data=COL.OLD, listw=lw)
summary(COL.SLX)
summary(impacts(COL.SLX))
COL.SLX <- lmSLX(CRIME ~ INC + HOVAL + I(HOVAL^2), data=COL.OLD, listw=lw, Durbin=TRUE)
summary(impacts(COL.SLX))
summary(COL.SLX)
COL.SLX <- lmSLX(CRIME ~ INC + HOVAL + I(HOVAL^2), data=COL.OLD, listw=lw, Durbin=~INC)
summary(impacts(COL.SLX))
```

```

summary(COL.SLX)
COL.SLX <- lmSLX(CRIME ~ INC, data=COL.OLD, listw=lw)
summary(COL.SLX)
summary(impacts(COL.SLX))
## Not run:
crds <- cbind(COL.OLD$X, COL.OLD$Y)
mdist <- sqrt(sum(diff(apply(crds, 2, range))^2))
dnb <- spdep::dnearest(crds, 0, mdist)
dists <- spdep::nb2listw(dnb, crds)
f <- function(x, form, data, dnb, dists, verbose) {
  glst <- lapply(dists, function(d) 1/(d^x))
  lw <- spdep::nb2listw(dnb, glist=glst, style="B")
  res <- logLik(lmSLX(form=form, data=data, listw=lw))
  if (verbose) cat("power:", x, "logLik:", res, "\n")
  res
}
opt <- optimize(f, interval=c(0.1, 4), form=CRIME ~ INC + HOVAL,
  data=COL.OLD, dnb=dnb, dists=dists, verbose=TRUE, maximum=TRUE)
glst <- lapply(dists, function(d) 1/(d^opt$maximum))
lw <- spdep::nb2listw(dnb, glist=glst, style="B")
SLX <- lmSLX(CRIME ~ INC + HOVAL, data=COL.OLD, listw=lw)
summary(SLX)
summary(impacts(SLX))

## End(Not run)
COL.SLX <- lmSLX(CRIME ~ INC + HOVAL, data=COL.OLD, listw=lw)
pslx0 <- predict(COL.SLX)
pslx1 <- predict(COL.SLX, newdata=COL.OLD, listw=lw)
all.equal(pslx0, pslx1)
COL.OLD1 <- COL.OLD
COL.OLD1$INC <- COL.OLD1$INC + 1
pslx2 <- predict(COL.SLX, newdata=COL.OLD1, listw=lw)
sum(coef(COL.SLX)[c(2,4)])
mean(pslx2-pslx1)

```

LR.Sarlm

Likelihood ratio test

Description

The `LR.Sarlm()` function provides a likelihood ratio test for objects for which a `logLik()` function exists for their class, or for objects of class `logLik`. `LR1.Sarlm()` and `Wald1.Sarlm()` are used internally in `summary.Sarlm()`, but may be accessed directly; they report the values respectively of LR and Wald tests for the absence of spatial dependence in spatial lag or error models. The spatial Hausman test is available for models fitted with `errorSarlm` and `GMerrorsar`.

Usage

```

LR.Sarlm(x, y)
## S3 method for class 'Sarlm'

```

```

logLik(object, ...)
LR1.Sarlm(object)
Wald1.Sarlm(object)
## S3 method for class 'Sarlm'
Hausman.test(object, ..., tol=NULL)
## S3 method for class 'Sarlm'
anova(object, ...)
bptest.Sarlm(object, varformula=NULL, studentize = TRUE, data=list())
## S3 method for class 'Sarlm'
impacts(obj, ..., tr, R = NULL, listw = NULL, evalues=NULL,
        useHESS = NULL, tol = 1e-06, empirical = FALSE, Q=NULL)

```

Arguments

x	a logLik object or an object for which a logLik() function exists
y	a logLik object or an object for which a logLik() function exists
object, obj	a Sarlm object
...	further arguments passed to or from other methods
varformula	a formula describing only the potential explanatory variables for the variance (no dependent variable needed). By default the same explanatory variables are taken as in the main regression model
studentize	logical. If set to TRUE Koenker's studentized version of the test statistic will be used.
data	an optional data frame containing the variables in the varformula
tr	A vector of traces of powers of the spatial weights matrix created using trW, for approximate impact measures; if not given, listw must be given for exact measures (for small to moderate spatial weights matrices); the traces must be for the same spatial weights as were used in fitting the spatial regression, and must be row-standardised
listw	If tr is not given, a spatial weights object as created by nb2listw; they must be the same spatial weights as were used in fitting the spatial regression, but do not have to be row-standardised
evalues	vector of eigenvalues of spatial weights matrix for impacts calculations
R	If given, simulations are used to compute distributions for the impact measures, returned as mcmc objects; the objects are used for convenience but are not output by an MCMC process
useHESS	Use the Hessian approximation (if available) even if the asymptotic coefficient covariance matrix is available; used for comparing methods
tol	Argument passed to mvrnorm and solve: tolerance (relative to largest variance) for numerical lack of positive-definiteness in the coefficient covariance matrix
empirical	Argument passed to mvrnorm (default FALSE): if true, the coefficients and their covariance matrix specify the empirical not population mean and covariance matrix
Q	default NULL, else an integer number of cumulative power series impacts to calculate if tr is given

Value

The tests return objects of class `htest` with:

<code>statistic</code>	value of statistic
<code>parameter</code>	degrees of freedom
<code>p.value</code>	Probability value
<code>estimate</code>	varies with test
<code>method</code>	description of test method

`logLik.Sarlm()` returns an object of class `logLik` LR1.Sarlm, Hausman.Sarlm and Wald1.Sarlm
 return objects of class `htest`

Note

The numbers of degrees of freedom returned by `logLik.Sarlm()` include nuisance parameters, that is the number of regression coefficients, plus sigma, plus spatial parameter estimate(s).

Author(s)

Roger Bivand <Roger.Bivand@nhh.no>, bptest: Torsten Hothorn and Achim Zeileis, modified by Roger Bivand

References

LeSage J and RK Pace (2009) Introduction to Spatial Econometrics. CRC Press, Boca Raton, pp. 61–63; Pace RK and LeSage J (2008) A spatial Hausman test. *Economics Letters* 101, 282–284.
 T.S. Breusch & A.R. Pagan (1979), A Simple Test for Heteroscedasticity and Random Coefficient Variation. *Econometrica* 47, 1287–1294
 W. Krämer & H. Sonnberger (1986), *The Linear Regression Model under Test*. Heidelberg: Physica.
 L. Anselin (1988) *Spatial econometrics: methods and models*. Dordrecht: Kluwer, pp. 121–122.

See Also

[logLik.lm](#), [anova.Sarlm](#)

Examples

```
require("sf", quietly=TRUE)
columbus <- st_read(system.file("shapes/columbus.gpkg", package="spData")[1], quiet=TRUE)
#require("spdep", quietly=TRUE)
col.gal.nb <- spdep::read.gal(system.file("weights/columbus.gal", package="spData")[1])
lm.mod <- lm(CRIME ~ HOVAL + INC, data=columbus)
lag <- lagsarlm(CRIME ~ HOVAL + INC, data=columbus, spdep::nb2listw(col.gal.nb))
mixed <- lagsarlm(CRIME ~ HOVAL + INC, data=columbus, spdep::nb2listw(col.gal.nb), type="mixed")
error <- errorsarlm(CRIME ~ HOVAL + INC, data=columbus, spdep::nb2listw(col.gal.nb))
Hausman.test(error)
LR.Sarlm(mixed, error)
anova(lag, lm.mod)
anova(lag, error, mixed)
```

```
AIC(lag, error, mixed)
bptest.Sarlm(error)
bptest.Sarlm(error, studentize=FALSE)
```

MCMCsamp

MCMC sample from fitted spatial regression

Description

The MCMCsamp method uses [rwmetrop](#), a random walk Metropolis algorithm, from **LearnBayes** to make MCMC samples from fitted maximum likelihood spatial regression models.

Usage

```
MCMCsamp(object, mcmc = 1L, verbose = NULL, ...)
## S3 method for class 'Spautolm'
MCMCsamp(object, mcmc = 1L, verbose = NULL, ...,
  burnin = 0L, scale=1, listw, control = list())
## S3 method for class 'Sarlm'
MCMCsamp(object, mcmc = 1L, verbose = NULL, ...,
  burnin=0L, scale=1, listw, listw2=NULL, control=list())
```

Arguments

object	A spatial regression model object fitted by maximum likelihood with spautolm
mcmc	The number of MCMC iterations after burnin
verbose	default NULL, use global option value; if TRUE, reports progress
...	Arguments passed through
burnin	The number of burn-in iterations for the sampler
scale	a positive scale parameter
listw, listw2	listw objects created for example by <code>nb2listw</code> ; should be the same object(s) used for fitting the model
control	list of extra control arguments - see spautolm

Value

An object of class “mcmc” suited to **coda**, with attributes: “accept” acceptance rate; “type” input ML fitted model type “SAR”, “CAR”, “SMA”, “lag”, “mixed”, “error”, “sac”, “sacmixed”; “timings” run times

Note

If the acceptance rate is below 0.05, a warning will be issued; consider increasing mcmc.

Author(s)

Roger Bivand <Roger.Bivand@nhh.no>

References

Jim Albert (2007) Bayesian Computation with R, Springer, New York, pp. 104-105.

See Also

[rwmetrop](#), [spautolm](#), [lagsarlm](#), [errorsarlm](#), [sacsarlm](#)

Examples

```
require("sf", quietly=TRUE)
nydata <- st_read(system.file("shapes/NY8_bna_utm18.gpkg", package="spData")[1], quiet=TRUE)
suppressMessages(nyadjmat <- as.matrix(foreign::read.dbf(system.file(
  "misc/nyadjwts.dbf", package="spData")[1])[-1]))
suppressMessages(ID <- as.character(names(foreign::read.dbf(system.file(
  "misc/nyadjwts.dbf", package="spData")[1]))[-1]))
identical(substr(ID, 2, 10), substr(as.character(nydata$AREAKEY), 2, 10))
#require("spdep", quietly=TRUE)
listw_NY <- spdep::mat2listw(nyadjmat, as.character(nydata$AREAKEY), style="B")
esar1f <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, family="SAR", method="eigen")
summary(esar1f)
res <- MCMCsamp(esar1f, mcmc=1000, burnin=200, listw=listw_NY)
summary(res)
## Not run:
esar1fw <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, weights=POP8, family="SAR", method="eigen")
summary(esar1fw)
res <- MCMCsamp(esar1fw, mcmc=5000, burnin=500, listw=listw_NY)
summary(res)
ecar1f <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, family="CAR", method="eigen")
summary(ecar1f)
res <- MCMCsamp(ecar1f, mcmc=5000, burnin=500, listw=listw_NY)
summary(res)
esar1fw <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, weights=POP8, family="SAR", method="eigen")
summary(esar1fw)
res <- MCMCsamp(esar1fw, mcmc=5000, burnin=500, listw=listw_NY)
summary(res)
ecar1fw <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, weights=POP8, family="CAR", method="eigen")
summary(ecar1fw)
res <- MCMCsamp(ecar1fw, mcmc=5000, burnin=500, listw=listw_NY)
summary(res)

## End(Not run)
esar0 <- errorsarlm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY)
summary(esar0)
res <- MCMCsamp(esar0, mcmc=1000, burnin=200, listw=listw_NY)
summary(res)
## Not run:
```

```

esar0w <- errorsarlm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, weights=POP8)
summary(esar0)
res <- MCMCsamp(esar0w, mcmc=5000, burnin=500, listw=listw_NY)
summary(res)
esar1 <- errorsarlm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, etype="emixed")
summary(esar1)
res <- MCMCsamp(esar1, mcmc=5000, burnin=500, listw=listw_NY)
summary(res)
lsar0 <- lagsarlm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY)
summary(lsar0)
res <- MCMCsamp(lsar0, mcmc=5000, burnin=500, listw=listw_NY)
summary(res)
lsar1 <- lagsarlm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, type="mixed")
summary(lsar1)
res <- MCMCsamp(lsar1, mcmc=5000, burnin=500, listw=listw_NY)
summary(res)
ssar0 <- sacsarlml(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY)
summary(ssar0)
res <- MCMCsamp(ssar0, mcmc=5000, burnin=500, listw=listw_NY)
summary(res)
ssar1 <- sacsarlml(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, type="sacmixed")
summary(ssar1)
res <- MCMCsamp(ssar1, mcmc=5000, burnin=500, listw=listw_NY)
summary(res)

## End(Not run)

```

ME

Moran eigenvector GLM filtering

Description

The Moran eigenvector filtering function is intended to remove spatial autocorrelation from the residuals of generalised linear models. It uses brute force eigenvector selection to reach a subset of such vectors to be added to the RHS of the GLM model to reduce residual autocorrelation to below the specified alpha value. Since eigenvector selection only works on symmetric weights, the weights are made symmetric before the eigenvectors are found (from `spdep` 0.5-50).

Usage

```

ME(formula, data=list(), family = gaussian, weights, offset,
  na.action=na.fail, listw=NULL, alpha=0.05, nsim=99, verbose=NULL,
  stdev=FALSE, zero.policy=NULL)

```

Arguments

formula	a symbolic description of the model to be fit
data	an optional data frame containing the variables in the model
family	a description of the error distribution and link function to be used in the model
weights	an optional vector of weights to be used in the fitting process
offset	this can be used to specify an a priori known component to be included in the linear predictor during fitting
na.action	a function (default <code>options("na.action")</code>), can also be <code>na.omit</code> or <code>na.exclude</code> with consequences for residuals and fitted values - in these cases the spatial weights list will be subsetted to remove NAs in the data. It may be necessary to set <code>zero.policy</code> to <code>TRUE</code> because this subsetting may create no-neighbour observations. Note that only weights lists created without using the <code>glist</code> argument to <code>nb2listw</code> may be subsetted.
listw	a <code>listw</code> object created for example by <code>nb2listw</code>
alpha	used as a stopping rule to choose all eigenvectors up to and including the one with a p-value exceeding alpha
nsim	number of permutations for permutation bootstrap for finding p-values
verbose	default <code>NULL</code> , use global option value; if <code>TRUE</code> report eigenvectors selected
stdev	if <code>TRUE</code> , p-value calculated from bootstrap permutation standard deviate using <code>pnorm</code> with <code>alternative="greater"</code> , if <code>FALSE</code> the Hope-type p-value
zero.policy	default <code>NULL</code> , use global option value; if <code>FALSE</code> stop with error for any empty neighbour sets, if <code>TRUE</code> permit the weights list to be formed with zero-length weights vectors

Details

The eigenvectors for inclusion are chosen by calculating the empirical Moran's I values for the initial model plus each of the doubly centred symmetric spatial weights matrix eigenvectors in turn. Then the first eigenvector is chosen as that with the lowest Moran's I value. The procedure is repeated until the lowest remaining Moran's I value has a permutation-based probability value above alpha. The probability value is either Hope-type or based on using the mean and standard deviation of the permutations to calculate ZI based on the `stdev` argument.

Value

An object of class `Me_res`:

selection	a matrix summarising the selection of eigenvectors for inclusion, with columns: Eigenvector number of selected eigenvector ZI permutation-based standardized deviate of Moran's I if <code>stdev=TRUE</code> pr(ZI) probability value: if <code>stdev=TRUE</code> of the permutation-based standardized deviate, if <code>FALSE</code> the Hope-type probability value, in both cases one-sided The first row is the value at the start of the search
vectors	a matrix of the selected eigenvectors in order of selection

Author(s)

Roger Bivand and Pedro Peres-Neto

References

Dray S, Legendre P and Peres-Neto PR (2005) Spatial modeling: a comprehensive framework for principle coordinate analysis of neighbor matrices (PCNM), *Ecological Modelling*; Griffith DA and Peres-Neto PR (2006) Spatial modeling in ecology: the flexibility of eigenfunction spatial analyses.

See Also

[SpatialFiltering, glm](#)

Examples

```
#require("spdep", quietly=TRUE)
data(hopkins, package="spData")
hopkins_part <- hopkins[21:36,36:21]
hopkins_part[which(hopkins_part > 0, arr.ind=TRUE)] <- 1
hopkins.rook.nb <- spdep::cell2nb(16, 16, type="rook")
glmbase <- glm(c(hopkins_part) ~ 1, family="binomial")
lw <- spdep::nb2listw(hopkins.rook.nb, style="B")
set.seed(123)
system.time(MEbinom1 <- ME(c(hopkins_part) ~ 1, family="binomial",
  listw=lw, alpha=0.05, verbose=TRUE, nsim=49))
glmME <- glm(c(hopkins_part) ~ 1 + fitted(MEbinom1), family="binomial")
#anova(glmME, test="Chisq")
coef(summary(glmME))
anova(glmbase, glmME, test="Chisq")
## Not run:
require("sf", quietly=TRUE)
columbus <- st_read(system.file("shapes/columbus.gpkg", package="spData")[1], quiet=TRUE)
#require("spdep", quietly=TRUE)
col.gal.nb <- spdep::read.gal(system.file("weights/columbus.gal", package="spData")[1])
lw <- spdep::nb2listw(col.gal.nb)
lmbase <- lm(CRIME ~ INC + HOVAL, data=columbus)
lagcol <- SpatialFiltering(CRIME ~ 1, ~ INC + HOVAL, data=columbus,
  nb=col.gal.nb, style="W", alpha=0.1, verbose=TRUE)
lagcol
lmlag <- lm(CRIME ~ INC + HOVAL + fitted(lagcol), data=columbus)
anova(lmbase, lmlag)
set.seed(123)
system.time(lagcol1 <- ME(CRIME ~ INC + HOVAL, data=columbus, family="gaussian",
  listw=lw, alpha=0.1, verbose=TRUE))
lagcol1
lmlag1 <- lm(CRIME ~ INC + HOVAL + fitted(lagcol1), data=columbus)
anova(lmbase, lmlag1)

set.seed(123)
lagcol2 <- ME(CRIME ~ INC + HOVAL, data=columbus, family="gaussian",
  listw=lw, alpha=0.1, stdev=TRUE, verbose=TRUE)
lagcol2
```

```

lmlag2 <- lm(CRIME ~ INC + HOVAL + fitted(lagcol2), data=columbus)
anova(lmbase, lmlag2)
NA.columbus <- columbus
NA.columbus$CRIME[20:25] <- NA
COL.ME.NA <- ME(CRIME ~ INC + HOVAL, data=NA.columbus, family="gaussian",
  listw=lw, alpha=0.1, stdev=TRUE, verbose=TRUE,
  na.action=na.exclude)
COL.ME.NA$na.action
summary(lm(CRIME ~ INC + HOVAL + fitted(COL.ME.NA), data=NA.columbus,
  na.action=na.exclude))
nc.sids <- st_read(system.file("shapes/sids.gpkg", package="spData")[1], quiet=TRUE)
rn <- as.character(nc.sids$FIPS)
ncCC89_nb <- spdep::read.gal(system.file("weights/ncCC89.gal", package="spData")[1],
  region.id=rn)
ncCR85_nb <- spdep::read.gal(system.file("weights/ncCR85.gal", package="spData")[1],
  region.id=rn)
glmbase <- glm(SID74 ~ 1, data=nc.sids, offset=log(BIR74),
  family="poisson")
set.seed(123)
MEpois1 <- ME(SID74 ~ 1, data=nc.sids, offset=log(BIR74),
  family="poisson", listw=spdep::nb2listw(ncCR85_nb, style="B"), alpha=0.2, verbose=TRUE)
MEpois1
glmME <- glm(SID74 ~ 1 + fitted(MEpois1), data=nc.sids, offset=log(BIR74),
  family="poisson")
anova(glmME, test="Chisq")
anova(glmbase, glmME, test="Chisq")

## End(Not run)

```

ML_models

Spatial simultaneous autoregressive model estimation by maximum likelihood

Description

The `lagsarlm` function provides Maximum likelihood estimation of spatial simultaneous autoregressive lag and spatial Durbin (mixed) models of the form:

$$y = \rho W y + X \beta + \varepsilon$$

where ρ is found by `optimize()` first, and β and other parameters by generalized least squares subsequently (one-dimensional search using `optim` performs badly on some platforms). In the spatial Durbin (mixed) model, the spatially lagged independent variables are added to X . Note that interpretation of the fitted coefficients should use impact measures, because of the feedback loops induced by the data generation process for this model. With one of the sparse matrix methods, larger numbers of observations can be handled, but the `interval=` argument may need be set when the weights are not row-standardised.

Maximum likelihood estimation of spatial simultaneous autoregressive error models of the form:

$$y = X\beta + u, u = \lambda W u + \varepsilon$$

where λ is found by `optimize()` first, and β and other parameters by generalized least squares subsequently. With one of the sparse matrix methods, larger numbers of observations can be handled, but the `interval=` argument may need be set when the weights are not row-standardised. When `etype` is “emixed”, a so-called spatial Durbin error model is fitted.

Maximum likelihood estimation of spatial simultaneous autoregressive “SAC/SARAR” models of the form:

$$y = \rho W^1 y + X\beta + u, u = \lambda W^2 u + \varepsilon$$

where ρ and λ are found by `nlnmb` or `optim()` first, and β and other parameters by generalized least squares subsequently.

Usage

```
lagsarlm(formula, data = list(), listw, na.action, Durbin, type,
  method="eigen", quiet=NULL, zero.policy=NULL, interval=NULL,
  tol.solve=.Machine$double.eps, trs=NULL, control=list())
errorsarlm(formula, data=list(), listw, na.action, weights=NULL,
  Durbin, etype, method="eigen", quiet=NULL, zero.policy=NULL,
  interval = NULL, tol.solve=.Machine$double.eps, trs=NULL, control=list())
sacsarlm(formula, data = list(), listw, listw2 = NULL, na.action, Durbin, type,
  method="eigen", quiet=NULL, zero.policy=NULL, tol.solve=.Machine$double.eps,
  llprof=NULL, interval1=NULL, interval2=NULL, trs1=NULL, trs2=NULL,
  control = list())
## S3 method for class 'Sarlm'
summary(object, correlation = FALSE, Nagelkerke = FALSE,
  Hausman=FALSE, adj.se=FALSE, ...)
## S3 method for class 'Sarlm'
print(x, ...)
## S3 method for class 'summary.Sarlm'
print(x, digits = max(5, .Options$digits - 3),
  signif.stars = FALSE, ...)
## S3 method for class 'Sarlm'
residuals(object, ...)
## S3 method for class 'Sarlm'
deviance(object, ...)
## S3 method for class 'Sarlm'
coef(object, ...)
## S3 method for class 'Sarlm'
vcov(object, ...)
## S3 method for class 'Sarlm'
fitted(object, ...)
```

Arguments

formula	a symbolic description of the model to be fit. The details of model specification are given for <code>lm()</code>
data	an optional data frame containing the variables in the model. By default the variables are taken from the environment which the function is called.
listw, listw2	a <code>listw</code> object created for example by <code>nb2listw</code> ; if <code>nb2listw</code> not given, set to the same spatial weights as the <code>listw</code> argument
na.action	a function (default <code>options("na.action")</code>), can also be <code>na.omit</code> or <code>na.exclude</code> with consequences for residuals and fitted values - in these cases the weights list will be subsetted to remove NAs in the data. It may be necessary to set <code>zero.policy</code> to <code>TRUE</code> because this subsetting may create no-neighbour observations. Note that only weights lists created without using the <code>glist</code> argument to <code>nb2listw</code> may be subsetted.
weights	an optional vector of weights to be used in the fitting process. Non-NULL weights can be used to indicate that different observations have different variances (with the values in weights being inversely proportional to the variances); or equivalently, when the elements of weights are positive integers w_i , that each response y_i is the mean of w_i unit-weight observations (including the case that there are w_i observations equal to y_i and the data have been summarized) - <code>lm</code>
Durbin	default <code>FALSE</code> (spatial lag model); if <code>TRUE</code> , full spatial Durbin model; if a formula object, the subset of explanatory variables to lag
type	(use the ‘Durbin=’ argument - retained for backwards compatibility only) default "lag", may be set to "mixed"; when "mixed", the lagged intercept is dropped for spatial weights style "W", that is row-standardised weights, but otherwise included; “Durbin” may be used instead of “mixed”
etype	(use the ‘Durbin=’ argument - retained for backwards compatibility only) default "error", may be set to "emixed" to include the spatially lagged independent variables added to X; when "emixed", the lagged intercept is dropped for spatial weights style "W", that is row-standardised weights, but otherwise included
method	"eigen" (default) - the Jacobian is computed as the product of $(1 - \rho * \text{eigenvalue})$ using <code>eigenw</code> , and "spam" or "Matrix_J" for strictly symmetric weights lists of styles "B" and "C", or made symmetric by similarity (Ord, 1975, Appendix C) if possible for styles "W" and "S", using code from the <code>spam</code> or <code>Matrix</code> packages to calculate the determinant; “Matrix” and “spam_update” provide updating Cholesky decomposition methods; "LU" provides an alternative sparse matrix decomposition approach. In addition, there are "Chebyshev" and Monte Carlo "MC" approximate log-determinant methods; the Smirnov/Anselin (2009) trace approximation is available as "moments". Three methods: "SE_classic", "SE_whichMin", and "SE_interp" are provided experimentally, the first to attempt to emulate the behaviour of Spatial Econometrics toolbox ML fitting functions. All use grids of log determinant values, and the latter two attempt to ameliorate some features of "SE_classic".
quiet	default <code>NULL</code> , use <code>!verbose</code> global option value; if <code>FALSE</code> , reports function values during optimization.

zero.policy	default NULL, use global option value; if TRUE assign zero to the lagged value of zones without neighbours, if FALSE (default) assign NA - causing lagsarlm() to terminate with an error
interval	default is NULL, search interval for autoregressive parameter
tol.solve	the tolerance for detecting linear dependencies in the columns of matrices to be inverted - passed to solve() (default=1.0e-10). This may be used if necessary to extract coefficient standard errors (for instance lowering to 1e-12), but errors in solve() may constitute indications of poorly scaled variables: if the variables have scales differing much from the autoregressive coefficient, the values in this matrix may be very different in scale, and inverting such a matrix is analytically possible by definition, but numerically unstable; rescaling the RHS variables alleviates this better than setting tol.solve to a very small value
llprof	default NULL, can either be an integer, to divide the feasible ranges into a grid of points, or a two-column matrix of spatial coefficient values, at which to evaluate the likelihood function
trs1, trs2	default NULL, if given, vectors for each weights object of powered spatial weights matrix traces output by trW; when given, used in some Jacobian methods
interval1, interval2	default is NULL, search intervals for each weights object for autoregressive parameters
trs	default NULL, if given, a vector of powered spatial weights matrix traces output by trW; when given, insert the asymptotic analytical values into the numerical Hessian instead of the approximated values; may be used to get around some problems raised when the numerical Hessian is poorly conditioned, generating NaNs in subsequent operations; the use of trs is recommended
control	list of extra control arguments - see section below
object	Sarlm object from lagsarlm, errorsarlm or sacsarlm
correlation	logical; if 'TRUE', the correlation matrix of the estimated parameters including sigma is returned and printed (default=FALSE)
Nagelkerke	if TRUE, the Nagelkerke pseudo R-squared is reported
Hausman	if TRUE, the results of the Hausman test for error models are reported
adj.se	if TRUE, adjust the coefficient standard errors for the number of fitted coefficients
x	Sarlm object from lagsarlm, errorsarlm or sacsarlm in print.Sarlm, summary object from summary.Sarlm for print.summary.Sarlm
digits	the number of significant digits to use when printing
signif.stars	logical. If TRUE, "significance stars" are printed for each coefficient.
...	further arguments passed to or from other methods

Details

The asymptotic standard error of ρ is only computed when method="eigen", because the full matrix operations involved would be costly for large n typically associated with the choice of

method="spam" or "Matrix". The same applies to the coefficient covariance matrix. Taken as the asymptotic matrix from the literature, it is typically badly scaled, and with the elements involving ρ (lag model) or λ (error model) being very small, while other parts of the matrix can be very large (often many orders of magnitude in difference). It often happens that the `tol.solve` argument needs to be set to a smaller value than the default, or the RHS variables can be centred or reduced in range.

Versions of the package from 0.4-38 include numerical Hessian values where asymptotic standard errors are not available. This change has been introduced to permit the simulation of distributions for impact measures. The warnings made above with regard to variable scaling also apply in this case.

Note that the `fitted()` function for the output object assumes that the response variable may be reconstructed as the sum of the trend, the signal, and the noise (residuals). Since the values of the response variable are known, their spatial lags are used to calculate signal components (Cressie 1993, p. 564). This differs from other software, including GeoDa, which does not use knowledge of the response variable in making predictions for the fitting data. Refer to the help page of `predict.Sarlm` for discussions and references.

Because numerical optimisation is used to find the values of λ and ρ in `sacsarlm`, care needs to be shown. It has been found that the surface of the 2D likelihood function often forms a “banana trench” from (low ρ , high λ) through (high ρ , high λ) to (high ρ , low λ) values. In addition, sometimes the banana has optima towards both ends, one local, the other global, and consequently the choice of the starting point for the final optimization becomes crucial. The default approach is not to use just (0, 0) as a starting point, nor the (ρ , λ) values from `gsts1s`, which lie in a central part of the “trench”, but either four values at (low ρ , high λ), (0, 0), (high ρ , high λ), and (high ρ , low λ), and to use the best of these start points for the final optimization. Optionally, nine points can be used spanning the whole (lower, upper) space.

Control arguments

tol.opt: the desired accuracy of the optimization - passed to `optimize()` (default=square root of double precision machine tolerance, a larger root may be used needed, see `help(boston)` for an example)

returnHcov: (error model) default TRUE, return the V_0 matrix for a spatial Hausman test

pWOrder: (error model) default 250, if `returnHcov=TRUE` and the method is not “eigen”, pass this order to `powerWeights` as the power series maximum limit

fdHess: default NULL, then set to (method != "eigen") internally; use `fdHess` to compute an approximate Hessian using finite differences when using sparse matrix methods; used to make a coefficient covariance matrix when the number of observations is large; may be turned off to save resources if need be

optimHess: default FALSE, use `fdHess` from **nlme**, if TRUE, use `optim` to calculate Hessian at optimum

optimHessMethod: default “optimHess”, may be “nlm” or one of the `optim` methods

compiled_sse: default FALSE; logical value used in the log likelihood function to choose compiled code for computing SSE

Imult: default 2; used for preparing the Cholesky decompositions for updating in the Jacobian function

super: if NULL (default), set to FALSE to use a simplicial decomposition for the sparse Cholesky decomposition and method “Matrix_J”, set to `as.logical(NA)` for method “Matrix”, if TRUE, use a supernodal decomposition

cheb_q: default 5; highest power of the approximating polynomial for the Chebyshev approximation

MC_p: default 16; number of random variates

MC_m: default 30; number of products of random variates matrix and spatial weights matrix

spamPivot: default “MMD”, alternative “RCM”

in_coef default 0.1, coefficient value for initial Cholesky decomposition in “spam_update”

type default “MC”, used with method “moments”; alternatives “mult” and “moments”, for use if `trs` is missing, `trW`

correct default TRUE, used with method “moments” to compute the Smirnov/Anselin correction term

trunc default TRUE, used with method “moments” to truncate the Smirnov/Anselin correction term

SE_method default “LU”, may be “MC”

nrho default 200, as in SE toolbox; the size of the first stage Indet grid; it may be reduced to for example 40

interp default 2000, as in SE toolbox; the size of the second stage Indet grid

small_asy default TRUE; if the method is not “eigen”, use asymmetric covariances rather than numerical Hessian ones if $n \leq \text{small}$

small default 1500; threshold number of observations for asymmetric covariances when the method is not “eigen”

SEIndet default NULL, may be used to pass a pre-computed SE toolbox style matrix of coefficients and their Indet values to the “SE_classic” and “SE_whichMin” methods

LU_order default FALSE; used in “LU_prepermutate”, note warnings given for lu method

pre_eig default NULL; may be used to pass a pre-computed vector of eigenvalues

return_impacts default TRUE; may be set FALSE to avoid problems calculating impacts with aliased variables

OrdVsign default 1; used to set the sign of the final component to negative if -1 (alpha times ((sigma squared) squared) in Ord (1975) equation B.1).

opt_method: default “nlnmb”, may be set to “L-BFGS-B” to use box-constrained optimisation in `optim`

opt_control: default `list()`, a control list to pass to `nlnmb` or `optim`

pars: default NULL, for which five trial starting values spanning the lower/upper range are tried and the best selected, starting values of ρ and λ

npars default integer 4L, four trial points; if not default value, nine trial points

pre_eig1, pre_eig2 default NULL; may be used to pass pre-computed vectors of eigenvalues

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References

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- Roger Bivand, Gianfranco Piras (2015). Comparing Implementations of Estimation Methods for Spatial Econometrics. *Journal of Statistical Software*, 63(18), 1-36. doi:10.18637/jss.v063.i18.
- Bivand, R. S., Hauke, J., and Kossowski, T. (2013). Computing the Jacobian in Gaussian spatial autoregressive models: An illustrated comparison of available methods. *Geographical Analysis*, 45(2), 150-179.

See Also

[lm](#), [impacts](#)

Examples

```
data(oldcol, package="spdep")
listw <- spdep::nb2listw(COL.nb, style="W")
ev <- eigenw(listw)
W <- as(listw, "CsparseMatrix")
trMatc <- trW(W, type="mult")
COL.lag.eig <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD, listw=listw,
  method="eigen", quiet=FALSE, control=list(pre_eig=ev, OrdVsign=1))
(x <- summary(COL.lag.eig, correlation=TRUE))
coef(x)
## Not run:
COL.lag.eig$fdHess
COL.lag.eig$resvar
# using the apparent sign in Ord (1975, equation B.1)
COL.lag.eigb <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD, listw=listw,
  method="eigen", control=list(pre_eig=ev, OrdVsign=-1))
summary(COL.lag.eigb)
COL.lag.eigb$fdHess
COL.lag.eigb$resvar
# force numerical Hessian
COL.lag.eig1 <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw=listw, method="Matrix", control=list(small=25))
summary(COL.lag.eig1)
COL.lag.eig1$fdHess
# force LeSage & Pace (2008, p. 57) approximation
COL.lag.eig1a <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw=listw, method="Matrix", control=list(small=25), trs=trMatc)
summary(COL.lag.eig1a)
```

```

COL.lag.eig1a$fdHess
COL.lag.eig$resvar[2,2]
# using the apparent sign in Ord (1975, equation B.1)
COL.lag.eigb$resvar[2,2]
# force numerical Hessian
COL.lag.eig1$fdHess[1,1]
# force LeSage & Pace (2008, p. 57) approximation
COL.lag.eig1a$fdHess[2,2]

## End(Not run)
system.time(COL.lag.M <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="Matrix", quiet=FALSE))
summary(COL.lag.M)
impacts(COL.lag.M, listw=listw)
## Not run:
system.time(COL.lag.sp <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw=listw, method="spam", quiet=FALSE))
summary(COL.lag.sp)
COL.lag.B <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  spdep::nb2listw(COL.nb, style="B"), control=list(pre_eig=ev))
summary(COL.lag.B)
COL.mixed.B <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  spdep::nb2listw(COL.nb, style="B"), type="mixed", tol.solve=1e-9,
  control=list(pre_eig=ev))
summary(COL.mixed.B)
COL.mixed.W <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, type="mixed", control=list(pre_eig=ev))
summary(COL.mixed.W)
COL.mixed.D00 <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, Durbin=TRUE, control=list(pre_eig=ev))
summary(COL.mixed.D00)
COL.mixed.D01 <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, Durbin=FALSE, control=list(pre_eig=ev))
summary(COL.mixed.D01)
COL.mixed.D1 <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, Durbin= ~ INC + HOVAL, control=list(pre_eig=ev))
summary(COL.mixed.D1)
f <- CRIME ~ INC + HOVAL
COL.mixed.D2 <- lagsarlm(f, data=COL.OLD, listw,
  Durbin=as.formula(delete.response(terms(f))),
  control=list(pre_eig=ev))
summary(COL.mixed.D2)
COL.mixed.D1a <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, Durbin= ~ INC, control=list(pre_eig=ev))
summary(COL.mixed.D1a)
try(COL.mixed.D1 <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, Durbin= ~ inc + HOVAL, control=list(pre_eig=ev)))
try(COL.mixed.D1 <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, Durbin= ~ DISCBD + HOVAL, control=list(pre_eig=ev)))
NA.COL.OLD <- COL.OLD
NA.COL.OLD$CRIME[20:25] <- NA
COL.lag.NA <- lagsarlm(CRIME ~ INC + HOVAL, data=NA.COL.OLD,
  listw, na.action=na.exclude)

```

```

COL.lag.NA$na.action
COL.lag.NA
resid(COL.lag.NA)
COL.lag.NA1 <- lagsarlm(CRIME ~ INC + HOVAL, data=NA.COL.OLD,
  listw, Durbin=~INC) # https://github.com/r-spatial/spatialreg/issues/10
COL.lag.NA1$na.action
COL.lag.NA2 <- lagsarlm(CRIME ~ INC + HOVAL, data=NA.COL.OLD,
  listw, Durbin=~INC, na.action=na.exclude)
COL.lag.NA2$na.action
# https://github.com/r-spatial/spatialreg/issues/11
COL.lag.NA3 <- lagsarlm(CRIME ~ INC + HOVAL, data=NA.COL.OLD,
  listw, control=list(pre_eig=ev))
COL.lag.NA3$na.action

## End(Not run)

## Not run:
data(boston, package="spData")
gp2mM <- lagsarlm(log(CMEDV) ~ CRIM + ZN + INDUS + CHAS + I(NOX^2) +
  I(RM^2) + AGE + log(DIS) + log(RAD) + TAX + PTRATIO + B + log(LSTAT),
  data=boston.c, spdep::nb2listw(boston.soi), type="mixed", method="Matrix")
summary(gp2mM)
W <- as(spdep::nb2listw(boston.soi), "CsparseMatrix")
trMatb <- trW(W, type="mult")
gp2mMi <- lagsarlm(log(CMEDV) ~ CRIM + ZN + INDUS + CHAS + I(NOX^2) +
  I(RM^2) + AGE + log(DIS) + log(RAD) + TAX + PTRATIO + B + log(LSTAT),
  data=boston.c, spdep::nb2listw(boston.soi), type="mixed", method="Matrix",
  trs=trMatb)
summary(gp2mMi)

## End(Not run)
COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, quiet=FALSE, control=list(pre_eig=ev))
summary(COL.errW.eig)
COL.errW.eig_ev <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, control=list(pre_eig=ev))
all.equal(coefficients(COL.errW.eig), coefficients(COL.errW.eig_ev))
COL.errB.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  spdep::nb2listw(COL.nb, style="B"))
summary(COL.errB.eig)
COL.errW.M <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="Matrix", quiet=FALSE, trs=trMatc)
summary(COL.errW.M)
COL.SDEM.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, etype="emixed", control=list(pre_eig=ev))
summary(COL.SDEM.eig)
## Not run:
COL.SDEM.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, Durbin=TRUE, control=list(pre_eig=ev))
summary(COL.SDEM.eig)
COL.SDEM.eig <- errorsarlm(CRIME ~ DISCBD + INC + HOVAL, data=COL.OLD,
  listw, Durbin=~INC, control=list(pre_eig=ev))
summary(COL.SDEM.eig)

```

```

summary(impacts(COL.SDEM.eig))
NA.COL.OLD <- COL.OLD
NA.COL.OLD$CRIME[20:25] <- NA
COL.err.NA <- errorsarlm(CRIME ~ INC + HOVAL, data=NA.COL.OLD,
  listw, na.action=na.exclude)
COL.err.NA$na.action
COL.err.NA
resid(COL.err.NA)
print(system.time(ev <- eigenw(similar.listw(listw))))
print(system.time(COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="eigen", control=list(pre_eig=ev))))
ocoef <- coefficients(COL.errW.eig)
print(system.time(COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="eigen", control=list(pre_eig=ev, LAPACK=FALSE))))
print(all.equal(ocoef, coefficients(COL.errW.eig)))
print(system.time(COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="eigen", control=list(pre_eig=ev, compiled_sse=TRUE))))
print(all.equal(ocoef, coefficients(COL.errW.eig)))
print(system.time(COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="Matrix_J", control=list(super=TRUE))))
print(all.equal(ocoef, coefficients(COL.errW.eig)))
print(system.time(COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="Matrix_J", control=list(super=FALSE))))
print(all.equal(ocoef, coefficients(COL.errW.eig)))
print(system.time(COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="Matrix_J", control=list(super=as.logical(NA)))))
print(all.equal(ocoef, coefficients(COL.errW.eig)))
print(system.time(COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="Matrix", control=list(super=TRUE))))
print(all.equal(ocoef, coefficients(COL.errW.eig)))
print(system.time(COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="Matrix", control=list(super=FALSE))))
print(all.equal(ocoef, coefficients(COL.errW.eig)))
print(system.time(COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="Matrix", control=list(super=as.logical(NA)))))
print(all.equal(ocoef, coefficients(COL.errW.eig)))
print(system.time(COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="spam", control=list(spamPivot="MMD"))))
print(all.equal(ocoef, coefficients(COL.errW.eig)))
print(system.time(COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="spam", control=list(spamPivot="RCM"))))
print(all.equal(ocoef, coefficients(COL.errW.eig)))
print(system.time(COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="spam_update", control=list(spamPivot="MMD"))))
print(all.equal(ocoef, coefficients(COL.errW.eig)))
print(system.time(COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, method="spam_update", control=list(spamPivot="RCM"))))
print(all.equal(ocoef, coefficients(COL.errW.eig)))

## End(Not run)
COL.sacW.eig <- sacsarlm(CRIME ~ INC + HOVAL, data=COL.OLD, listw,
  control=list(pre_eig1=ev, pre_eig2=ev))
summary(COL.sacW.eig)

```

```

set.seed(1)
summary(impacts(COL.sacW.eig, tr=trMatc, R=2000), zstats=TRUE, short=TRUE)
COL.msacW.eig <- sacsarlms(CRIME ~ INC + HOVAL, data=COL.OLD, listw,
  type="sacmixed", control=list(pre_eig1=ev, pre_eig2=ev))
summary(COL.msacW.eig)
set.seed(1)
summary(impacts(COL.msacW1.eig, tr=trMatc, R=2000), zstats=TRUE, short=TRUE)
COL.msacW1.eig <- sacsarlms(CRIME ~ INC + HOVAL, data=COL.OLD, listw,
  Durbin=TRUE, control=list(pre_eig1=ev, pre_eig2=ev))
summary(COL.msacW1.eig)
set.seed(1)
summary(impacts(COL.msacW2.eig, tr=trMatc, R=2000), zstats=TRUE, short=TRUE)
COL.msacW2.eig <- sacsarlms(CRIME ~ DISCBD + INC + HOVAL, data=COL.OLD,
  listw, Durbin= ~ INC, control=list(pre_eig1=ev, pre_eig2=ev))
summary(COL.msacW2.eig)
summary(impacts(COL.msacW2.eig, tr=trMatc, R=2000), zstats=TRUE, short=TRUE)
## Not run:
COL.mix.eig <- lagsarlms(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, type="mixed", method="eigen")
summary(COL.mix.eig, correlation=TRUE, Nagelkerke=TRUE)
COL.mix.M <- lagsarlms(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw, type="mixed", method="Matrix")
summary(COL.mix.M, correlation=TRUE, Nagelkerke=TRUE)
COL.errW.eig <- errorsarlms(CRIME ~ INC + HOVAL, data=COL.OLD,
  spdep::nb2listw(COL.nb, style="W"), method="eigen")
summary(COL.errW.eig, correlation=TRUE, Nagelkerke=TRUE, Hausman=TRUE)

## End(Not run)

```

predict.Sarlm	<i>Prediction for spatial simultaneous autoregressive linear model objects</i>
---------------	--

Description

predict.Sarlm() calculates predictions as far as is at present possible for for spatial simultaneous autoregressive linear model objects, using Haining's terminology for decomposition into trend, signal, and noise, or other types of predictors — see references.

Usage

```

## S3 method for class 'Sarlm'
predict(object, newdata = NULL, listw = NULL, pred.type = "TS", all.data = FALSE,
  zero.policy = NULL, legacy = TRUE, legacy.mixed = FALSE, power = NULL, order = 250,
  tol = .Machine$double.eps^(3/5), spChk = NULL, ...)
#\method{predict}{SLX}(object, newdata, listw, zero.policy=NULL, ...)
## S3 method for class 'Sarlm.pred'
print(x, ...)
## S3 method for class 'Sarlm.pred'
as.data.frame(x, ...)

```

Arguments

object	Sarlm object returned by lagsarlm, errorsarlm or sacsarlm, the method for SLX objects takes the output of lmSLX
newdata	data frame in which to predict — if NULL, predictions are for the data on which the model was fitted. Should have row names corresponding to region.id. If row names are exactly the same than the ones used for training, it uses in-sample predictors for forecast. See ‘Details’
listw	a listw object created for example by nb2listw. In the out-of-sample prediction case (ie. if newdata is not NULL), if legacy.mixed=FALSE or if pred.type!="TS", it should include both in-sample and out-of-sample spatial units. In this case, if regions of the listw are not in the correct order, they are reordered. See ‘Details’
pred.type	predictor type — default “TS”, use decomposition into trend, signal, and noise ; other types available depending on newdata. If newdata=NULL (in-sample prediction), “TS”, “trend”, “TC” and “BP” are available. If newdata is not NULL and its row names are the same than the data used to fit the model (forecast case), “TS”, “trend” and “TC” are available. In other cases (out-of-sample prediction), “TS”, “trend”, “KP1”, “KP2”, “KP3”, “KP4”, “KP5”, “TC”, “BP”, “BPW”, “BPN”, “TS1”, “TC1”, “BP1”, “BPW1” and “BPN1” are available. See ‘Details’ and references
all.data	(only applies to pred.type="TC" and newdata is not NULL) default FALSE: return predictions only for newdata units, if TRUE return predictions for all data units. See ‘Details’
zero.policy	default NULL, use global option value; if TRUE assign zero to the lagged value of zones without neighbours, if FALSE (default) assign NA - causing the function to terminate with an error
legacy	(only applies to lag and Durbin (mixed) models for pred.type="TS") default TRUE: use ad-hoc predictor, if FALSE use DGP-based predictor
legacy.mixed	(only applies to mixed models if newdata is not NULL) default FALSE: compute lagged variables from both in-sample and out-of-sample units with $[WX]_O$ and $[WX]_S$ where $X=cbind(X_s, X_o)$, if TRUE compute lagged variables independently between in-sample and out-of-sample units with $W_{OO}X_O$ and $W_{SS}X_S$
power	(only applies to lag and Durbin (mixed) models for “TS”, “KP1”, “KP2”, “KP3”, “TC”, “TC1”, “BP”, “BP1”, “BPN”, “BPN1”, “BPW” and “BPW1” types) use powerWeights, if default NULL, set FALSE if object\$method is “eigen”, otherwise TRUE
order	power series maximum limit if power is TRUE
tol	tolerance for convergence of power series if power is TRUE
spChk	should the row names of data frames be checked against the spatial objects for identity integrity, TRUE, or FALSE, default NULL to use get.spChkOption()
x	the object to be printed
...	further arguments passed through

Details

The function supports three types of prediction. In-sample prediction is the computation of predictors on the data used to fit the model (`newdata=NULL`). Prevision, also called forecast, is the computation of some predictors (“trend”, in-sample “TC” and out-of-sample “TS”) on the same spatial units than the ones used to fit the model, but with different observations of the variables in the model (row names of `newdata` should have the same row names than the data frame used to fit the model). And out-of-sample prediction is the computation of predictors on other spatial units than the ones used to fit the model (`newdata` has different row names). For extensive definitions, see Goulard et al. (2017).

`pred.type` of predictors are available according to the model of object and to the type of prediction. In the two following tables, “yes” means that the predictor can be used with the model, “no” means that `predict.Sarlm()` will stop with an error, and “yes*” means that the predictor is not designed for the specified model, but it can be used with `predict.Sarlm()`. In the last case, be careful with the computation of an inappropriate predictor.

In-sample predictors by models

pred.type	sem (mixed)	lag (mixed)	sac (mixed)
“trend”	yes	yes	yes
“TS”	yes	yes	no
“TC”	no	yes	yes*
“BP”	no	yes	yes*

Note that only “trend” and “TC” are available for prevision.

Out-of-sample predictors by models

pred.type	sem (mixed)	lag (mixed)	sac (mixed)
“trend”	yes	yes	yes
“TS”	yes	yes	no
“TS1” or “KP4”	no	yes	yes
“TC”	no	yes	yes*
“TC1” or “KP1”	yes	yes	yes
“BP”	no	yes	yes*
“BP1”	no	yes	yes*
“BPW”	no	yes	yes*
“BPW1”	no	yes	yes*
“BN”	no	yes	yes*
“BPN1”	no	yes	yes*
“KP2”	yes	yes	yes
“KP3”	yes	yes	yes
“KP5”	yes	no	yes*

Values for `pred.type=` include “TS1”, “TC”, “TC1”, “BP”, “BP1”, “BPW”, “BPW1”, “BPN”, “BPN1”, following the notation in Goulard et al. (2017), and for `pred.type=` “KP1”, “KP2”,

“KP3”, “KP4”, “KP5”, following the notation in Kelejian et al. (2007). `pred.type="TS"` is described below and in Bivand (2002).

In the following, the trend is the non-spatial smooth, the signal is the spatial smooth, and the noise is the residual. The fit returned by `pred.type="TS"` is the sum of the trend and the signal.

When `pred.type="TS"`, the function approaches prediction first by dividing invocations between those with or without newdata. When no newdata is present, the response variable may be reconstructed as the sum of the trend, the signal, and the noise (residuals). Since the values of the response variable are known, their spatial lags are used to calculate signal components (Cressie 1993, p. 564). For the error model, $\text{trend} = X\beta$, and $\text{signal} = \lambda W y - \lambda W X\beta$. For the lag and mixed models, $\text{trend} = X\beta$, and $\text{signal} = \rho W y$.

This approach differs from the design choices made in other software, for example GeoDa, which does not use observations of the response variable, and corresponds to the newdata situation described below.

When however newdata is used for prediction, no observations of the response variable being predicted are available. Consequently, while the trend components are the same, the signal cannot take full account of the spatial smooth. In the error model and Durbin error model, the signal is set to zero, since the spatial smooth is expressed in terms of the error: $(I - \lambda W)^{-1}\varepsilon$.

In the lag model, the signal can be expressed in the following way (for `legacy=TRUE`):

$$\begin{aligned}(I - \rho W)y &= X\beta + \varepsilon \\ y &= (I - \rho W)^{-1}X\beta + (I - \rho W)^{-1}\varepsilon\end{aligned}$$

giving a feasible signal component of:

$$\rho W y = \rho W (I - \rho W)^{-1} X\beta$$

For `legacy=FALSE`, the trend is computed first as:

$$X\beta$$

next the prediction using the DGP:

$$(I - \rho W)^{-1} X\beta$$

and the signal is found as the difference between prediction and trend. The numerical results for the legacy and DGP methods are identical.

setting the error term to zero. This also means that predictions of the signal component for lag and mixed models require the inversion of an n-by-n matrix.

Because the outcomes of the spatial smooth on the error term are unobservable, this means that the signal values for newdata are incomplete. In the mixed model, the spatially lagged RHS variables influence both the trend and the signal, so that the root mean square prediction error in the examples below for this case with newdata is smallest, although the model was not the best fit.

If newdata has more than one row, leave-one-out predictors (`pred.type=` include “TS1”, “TC1”, “BP1”, “BPW1”, “BPN1”, “KP1”, “KP2”, “KP3”, “KP4”, “KP5”) are computed separately on each out-of-sample unit.

listw should be provided except if newdata=NULL and pred.type= include "TS", "trend", or if newdata is not NULL, pred.type="trend" and object is not a mixed model.

all.data is useful when some out-of-sample predictors return different predictions for in-sample units, than the same predictor type computed only on in-sample data.

Value

predict.Sarlm() returns a vector of predictions with three attribute vectors of trend, signal (only for pred.type="TS") and region.id values and two other attributes of pred.type and call with class Sarlm.pred.

print.Sarlm.pred() is a print function for this class, printing and returning a data frame with columns: "fit", "trend" and "signal" (when available) and with region.id as row names.

Author(s)

Roger Bivand <Roger.Bivand@nhh.no> and Martin Gubri

References

Haining, R. 1990 *Spatial data analysis in the social and environmental sciences*, Cambridge: Cambridge University Press, p. 258; Cressie, N. A. C. 1993 *Statistics for spatial data*, Wiley, New York; Michel Goulard, Thibault Laurent & Christine Thomas-Agnan, 2017 *About predictions in spatial autoregressive models: optimal and almost optimal strategies*, Spatial Economic Analysis Volume 12, Issue 2–3, 304–325 doi:10.1080/17421772.2017.1300679, ; Kelejjan, H. H. and Prucha, I. R. 2007 *The relative efficiencies of various predictors in spatial econometric models containing spatial lags*, Regional Science and Urban Economics, Volume 37, Issue 3, 363–374; Bivand, R. 2002 *Spatial econometrics functions in R: Classes and methods*, Journal of Geographical Systems, Volume 4, No. 4, 405–421

See Also

[errorsarlm](#), [lagsarlm](#), [sacsarlm](#)

Examples

```
data(oldcol, package="spdep")
lw <- spdep::nb2listw(COL.nb)
COL.lag.eig <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD, lw)

COL.mix.eig <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD, lw,
  type="mixed")
print(p1 <- predict(COL.mix.eig))
print(p2 <- predict(COL.mix.eig, newdata=COL.OLD, listw=lw, pred.type = "TS",
  legacy.mixed = TRUE))
AIC(COL.mix.eig)
sqrt(deviance(COL.mix.eig)/length(COL.nb))
sqrt(sum((COL.OLD$CRIME - as.vector(p1))^2)/length(COL.nb))
sqrt(sum((COL.OLD$CRIME - as.vector(p2))^2)/length(COL.nb))

COL.err.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD, lw)
```

```

AIC(COL.err.eig)
sqrt(deviance(COL.err.eig)/length(COL.nb))
sqrt(sum((COL.OLD$CRIME - as.vector(predict(COL.err.eig)))^2)/length(COL.nb))
sqrt(sum((COL.OLD$CRIME - as.vector(predict(COL.err.eig, newdata=COL.OLD,
  listw=lw, pred.type = "TS")))^2)/length(COL.nb))

COL.SDerr.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD, lw,
  etype="emixed")
AIC(COL.SDerr.eig)
sqrt(deviance(COL.SDerr.eig)/length(COL.nb))
sqrt(sum((COL.OLD$CRIME - as.vector(predict(COL.SDerr.eig)))^2)/length(COL.nb))
sqrt(sum((COL.OLD$CRIME - as.vector(predict(COL.SDerr.eig, newdata=COL.OLD,
  listw=lw, pred.type = "TS")))^2)/length(COL.nb))

AIC(COL.lag.eig)
sqrt(deviance(COL.lag.eig)/length(COL.nb))
sqrt(sum((COL.OLD$CRIME - as.vector(predict(COL.lag.eig)))^2)/length(COL.nb))
sqrt(sum((COL.OLD$CRIME - as.vector(predict(COL.lag.eig, newdata=COL.OLD,
  listw=lw, pred.type = "TS")))^2)/length(COL.nb))

p3 <- predict(COL.mix.eig, newdata=COL.OLD, listw=lw, pred.type = "TS",
  legacy=FALSE, legacy.mixed = TRUE)
all.equal(p2, p3, check.attributes=FALSE)
p4 <- predict(COL.mix.eig, newdata=COL.OLD, listw=lw, pred.type = "TS",
  legacy=FALSE, power=TRUE, legacy.mixed = TRUE)
all.equal(p2, p4, check.attributes=FALSE)
p5 <- predict(COL.mix.eig, newdata=COL.OLD, listw=lw, pred.type = "TS",
  legacy=TRUE, power=TRUE, legacy.mixed = TRUE)
all.equal(p2, p5, check.attributes=FALSE)

```

set.mcOption

Options for parallel support

Description

Provides support for the use of parallel computation in the parallel package.

Usage

```

set.mcOption(value)
get.mcOption()
set.coresOption(value)
get.coresOption()
set.ClusterOption(cl)
get.ClusterOption()

```

Arguments

value	valid replacement value
cl	a cluster object created by makeCluster in parallel

Details

Options in the `spatialreg` package are held in an environment local to the package namespace and not exported. Option values are set and retrieved with pairs of access functions, `get` and `set`. The `mc` option is set by default to `FALSE` on Windows systems, as they cannot fork the R session; by default it is `TRUE` on other systems, but may be set `FALSE`. If `mc` is `FALSE`, the `Cluster` option is used: if `mc` is `FALSE` and the `Cluster` option is `NULL` no parallel computing is done, or the `Cluster` option is passed a “cluster” object created by the `parallel` or `snow` package for access without being passed as an argument. The `cores` option is set to `NULL` by default, and can be used to store the number of cores to use as an integer. If `cores` is `NULL`, facilities from the `parallel` package will not be used.

Value

The option access functions return their current settings, the assignment functions usually return the previous value of the option.

Note

An extended example is shown in the documentation of `mom_calc`, including treatment of seeding of RNG for multicore/cluster.

Author(s)

Roger Bivand <Roger.Bivand@nhh.no>

Examples

```
ls(envir=spatialreg:::.spatialregOptions)
library(parallel)
nc <- max(2L, detectCores(logical=FALSE), na.rm = TRUE)-1L
nc
# set nc to 1L here
if (nc > 1L) nc <- 1L
#nc <- ifelse(nc > 2L, 2L, nc)
coresOpt <- get.coresOption()
coresOpt
if (!is.na(nc)) {
  invisible(set.coresOption(nc))
  print(exists("mom_calc"))
  if(.Platform$OS.type == "windows") {
# forking not permitted on Windows - start cluster
# removed for Github actions 210502
## Not run:
    print(get.mcOption())
    cl <- makeCluster(get.coresOption())
    print(clusterEvalQ(cl, exists("mom_calc")))
    set.ClusterOption(cl)
    clusterEvalQ(get.ClusterOption(), library(spatialreg))
    print(clusterEvalQ(cl, exists("mom_calc")))
    clusterEvalQ(get.ClusterOption(), detach(package:spatialreg))
    set.ClusterOption(NULL)
  }
```

```

print(clusterEvalQ(cl, exists("mom_calc")))
stopCluster(cl)

## End(Not run)
} else {
  mcOpt <- get.mcOption()
  print(mcOpt)
  print(mclapply(1:get.coresOption(), function(i) exists("mom_calc"),
    mc.cores=get.coresOption()))
  invisible(set.mcOption(FALSE))
  cl <- makeCluster(nc)
  print(clusterEvalQ(cl, exists("mom_calc")))
  set.ClusterOption(cl)
  clusterEvalQ(get.ClusterOption(), library(spatialreg))
  print(clusterEvalQ(cl, exists("mom_calc")))
  clusterEvalQ(get.ClusterOption(), detach(package:spatialreg))
  set.ClusterOption(NULL)
  print(clusterEvalQ(cl, exists("mom_calc")))
  stopCluster(cl)
  invisible(set.mcOption(mcOpt))
}
invisible(set.coresOption(coresOpt))
}

```

set.ZeroPolicyOption *Control checking of spatial object IDs*

Description

Provides support for checking the mutual integrity of spatial neighbour weights and spatial data; similar mechanisms are used for passing global verbose and zero.policy options, and for providing access to a running cluster for embarrassingly parallel tasks.

Usage

```

set.VerboseOption(check)
get.VerboseOption()
set.ZeroPolicyOption(check)
get.ZeroPolicyOption()
#set.listw_is_CsparseMatrix_Option(check)
#get.listw_is_CsparseMatrix_Option()

```

Arguments

check a logical value, TRUE or FALSE

Details

Analysis functions will have an `spChk` argument by default set to `NULL`, and will call `get.spChkOption()` to get the global spatial option for whether to check or not — this is initialised to `FALSE`, and consequently should not break anything. It can be changed to `TRUE` using `set.spChkOption(TRUE)`, or the `spChk` argument can be assigned in analysis functions. `spNamedVec()` is provided to ensure that rownames are passed on to single columns taken from two-dimensional arrays and data frames.

Value

`set.spChkOption()` returns the old logical value, `get.spChkOption()` returns the current logical value, and `chkIDs()` returns a logical value for the test lack of difference. `spNamedVec()` returns the selected column with the names set to the row names of the object from which it has been extracted.

Author(s)

Roger Bivand <Roger.Bivand@nhh.no>

Examples

```
get.VerboseOption()
get.ZeroPolicyOption()
```

similar.listw

Create symmetric similar weights lists

Description

From Ord's 1975 paper, it is known that the Jacobian for SAR models may be found by "symmetrizing" by similarity (the eigenvalues of similar matrices are identical, so the Jacobian is too). This applies only to styles "W" and "S" with underlying symmetric binary neighbour relations or symmetric general neighbour relations (so no k-nearest neighbour relations). The function is invoked automatically within the SAR fitting functions, to call `eigen` on a symmetric matrix for the default eigen method, or to make it possible to use the Matrix method on weights that can be "symmetrized" in this way.

Usage

```
similar.listw(listw)
```

Arguments

`listw` a listw object created for example by `spdep::nb2listw`

Value

a listw object

Author(s)

Roger Bivand <Roger.Bivand@nhh.no>

References

Ord, J. K. 1975 Estimation methods for models of spatial interaction, *Journal of the American Statistical Association*, 70, 120-126

See Also

[lagsarlm](#), [errorsarlm](#)

Examples

```
#require("spdep", quietly=TRUE)
data(oldcol, package="spdep")
COL.W <- spdep::nb2listw(COL.nb, style="W")
COL.S <- spdep::nb2listw(COL.nb, style="S")
sum(log(1 - 0.5 * eigenw(COL.W)))
sum(log(1 - 0.5 * eigenw(similar.listw(COL.W))))
W_J <- as(as_dsTMatrix_listw(similar.listw(COL.W)), "CsparseMatrix")
I <- as_dsCMatrix_I(dim(W_J)[1])
c(determinant(I - 0.5 * W_J, logarithm=TRUE)$modulus)
sum(log(1 - 0.5 * eigenw(COL.S)))
sum(log(1 - 0.5 * eigenw(similar.listw(COL.S))))
W_J <- as(as_dsTMatrix_listw(similar.listw(COL.S)), "CsparseMatrix")
c(determinant(I - 0.5 * W_J, logarithm=TRUE)$modulus)
```

SpatialFiltering

Semi-parametric spatial filtering

Description

The function selects eigenvectors in a semi-parametric spatial filtering approach to removing spatial dependence from linear models. Selection is by brute force by finding the single eigenvector reducing the standard variate of Moran's I for regression residuals most, and continuing until no candidate eigenvector reduces the value by more than `tol`. It returns a summary table from the selection process and a matrix of selected eigenvectors for the specified model.

Usage

```
SpatialFiltering(formula, lagformula=NULL, data=list(), na.action=na.fail,
  nb=NULL, glist = NULL,
  style = "C", zero.policy = NULL, tol = 0.1, zerovalue = 1e-04,
  ExactEV = FALSE, symmetric = TRUE, alpha=NULL, alternative="two.sided",
  verbose=NULL)
```

Arguments

formula	a symbolic description of the model to be fit, assuming a spatial error representation; when lagformula is given, it should include only the response and the intercept term
lagformula	An extra one-sided formula to be used when a spatial lag representation is desired; the intercept is excluded within the function if present because it is part of the formula argument, but excluding it explicitly in the lagformula argument in the presence of factors generates a collinear model matrix
data	an optional data frame containing the variables in the model
nb	an object of class nb
glist	list of general weights corresponding to neighbours
style	style can take values W, B, C, U, and S
na.action	a function (default options("na.action")), can also be na.omit or na.exclude with consequences for residuals and fitted values - in these cases the spatial weights list will be subsetted to remove NAs in the data. It may be necessary to set zero.policy to TRUE because this subsetting may create no-neighbour observations. Note that only weights lists created without using the glist argument to nb2listw may be subsetted.
zero.policy	default NULL, use global option value; if FALSE stop with error for any empty neighbour sets, if TRUE permit the weights list to be formed with zero-length weights vectors
tol	tolerance value for convergence of spatial filtering
zerovalue	eigenvectors with eigenvalues of an absolute value smaller than zerovalue will be excluded in eigenvector search
ExactEV	Set ExactEV=TRUE to use exact expectations and variances rather than the expectation and variance of Moran's I from the previous iteration, default FALSE
symmetric	Should the spatial weights matrix be forced to symmetry, default TRUE
alpha	if not NULL, used instead of the tol= argument as a stopping rule to choose all eigenvectors up to and including the one with a probability value exceeding alpha.
alternative	a character string specifying the alternative hypothesis, must be one of greater, less or two.sided (default).
verbose	default NULL, use global option value; if TRUE report eigenvectors selected

Value

An SfResult object, with:

selection	a matrix summarising the selection of eigenvectors for inclusion, with columns: Step Step counter of the selection procedure SelEvec number of selected eigenvector (sorted descending) Eval its associated eigenvalue MinMi value Moran's I for residual autocorrelation
-----------	---

ZMinMi standardized value of Moran's I assuming a normal approximation
pr(ZI) probability value of the permutation-based standardized deviate for the given value of the alternative argument
R2 R² of the model including exogenous variables and eigenvectors
gamma regression coefficient of selected eigenvector in fit
The first row is the value at the start of the search
dataset a matrix of the selected eigenvectors in order of selection

Author(s)

Yongwan Chun, Michael Tiefelsdorf, Roger Bivand

References

Tiefelsdorf M, Griffith DA. (2007) Semiparametric Filtering of Spatial Autocorrelation: The Eigenvector Approach. *Environment and Planning A*, 39 (5) 1193 - 1221.

See Also

[lm](#), [eigen](#), [nb2listw](#), [listw2U](#)

Examples

```
require("sf", quietly=TRUE)
columbus <- st_read(system.file("shapes/columbus.gpkg", package="spData"))[1], quiet=TRUE)
#require("spdep", quietly=TRUE)
col.gal.nb <- spdep::read.gal(system.file("weights/columbus.gal", package="spData"))[1])
lmbase <- lm(CRIME ~ INC + HOVAL, data=columbus)
sarcol <- SpatialFiltering(CRIME ~ INC + HOVAL, data=columbus,
  nb=col.gal.nb, style="W", ExactEV=TRUE)
sarcol
lmsar <- lm(CRIME ~ INC + HOVAL + fitted(sarcol), data=columbus)
(x <- summary(lmsar))
coef(x)
anova(lmbase, lmsar)
spdep::lm.morantest(lmsar, spdep::nb2listw(col.gal.nb))
lagcol <- SpatialFiltering(CRIME ~ 1, ~ INC + HOVAL - 1, data=columbus,
  nb=col.gal.nb, style="W")
lagcol
lmlag <- lm(CRIME ~ INC + HOVAL + fitted(lagcol), data=columbus)
lmlag
anova(lmbase, lmlag)
spdep::lm.morantest(lmlag, spdep::nb2listw(col.gal.nb))
NA.columbus <- columbus
NA.columbus$CRIME[20:25] <- NA
COL.SF.NA <- SpatialFiltering(CRIME ~ INC + HOVAL, data=NA.columbus,
  nb=col.gal.nb, style="W", na.action=na.exclude)
COL.SF.NA$na.action
summary(lm(CRIME ~ INC + HOVAL + fitted(COL.SF.NA), data=NA.columbus,
  na.action=na.exclude))
```

spautolm

*Spatial conditional and simultaneous autoregression model estimation***Description**

Function taking family and weights arguments for spatial autoregression model estimation by Maximum Likelihood, using dense matrix methods, not suited to large data sets with thousands of observations. With one of the sparse matrix methods, larger numbers of observations can be handled, but the `interval=` argument should be set. The implementation is GLS using the single spatial coefficient value, here termed `lambda`, found by line search using `optimize` to maximise the log likelihood.

Usage

```
spautolm(formula, data = list(), listw, weights,
na.action, family = "SAR", method="eigen", verbose = NULL, trs=NULL,
interval=NULL, zero.policy = NULL, tol.solve=.Machine$double.eps,
llprof=NULL, control=list())
## S3 method for class 'Spautolm'
summary(object, correlation = FALSE, adj.se=FALSE,
Nagelkerke=FALSE, ...)
```

Arguments

<code>formula</code>	a symbolic description of the model to be fit. The details of model specification are given for <code>lm()</code>
<code>data</code>	an optional data frame containing the variables in the model. By default the variables are taken from the environment which the function is called.
<code>listw</code>	a <code>listw</code> object created for example by <code>nb2listw</code>
<code>weights</code>	an optional vector of weights to be used in the fitting process
<code>na.action</code>	a function (default <code>options("na.action")</code>), can also be <code>na.omit</code> or <code>na.exclude</code> with consequences for residuals and fitted values - in these cases the weights list will be subsetted to remove NAs in the data. Note that only weights lists created without using the <code>glist</code> argument to <code>nb2listw</code> may be subsetted.
<code>family</code>	character string: either "SAR" or "CAR" for simultaneous or conditional autoregressions; "SMA" for spatial moving average added thanks to Jielai Ma - "SMA" is only implemented for <code>method="eigen"</code> because it necessarily involves dense matrices
<code>method</code>	character string: default "eigen" for use of dense matrices, "Matrix_J" for sparse matrices (restricted to spatial weights symmetric or similar to symmetric) using methods in the Matrix package; "Matrix" provides updating Cholesky decomposition methods. Values of <code>method</code> may also include "LU", which provides an alternative sparse matrix decomposition approach, and the "Chebyshev" and Monte Carlo "MC" approximate log-determinant methods.

<code>verbose</code>	default NULL, use global option value; if TRUE, reports function values during optimization.
<code>trs</code>	default NULL, if given, a vector of powered spatial weights matrix traces output by <code>trW</code> ; when given, used in some Jacobian methods
<code>interval</code>	search interval for autoregressive parameter when not using <code>method="eigen"</code> ; default is <code>c(-1,0.999)</code> , <code>optimize</code> will reset NA/NaN to a bound and gives a warning when the interval is poorly set; <code>method="Matrix"</code> will attempt to search for an appropriate interval, if <code>find_interval=TRUE</code> (fails on some platforms)
<code>zero.policy</code>	default NULL, use global option value; Include list of no-neighbour observations in output if TRUE — otherwise <code>zero.policy</code> is handled within the <code>listw</code> argument
<code>tol.solve</code>	the tolerance for detecting linear dependencies in the columns of matrices to be inverted - passed to <code>solve()</code> (default=double precision machine tolerance). Errors in <code>solve()</code> may constitute indications of poorly scaled variables: if the variables have scales differing much from the autoregressive coefficient, the values in this matrix may be very different in scale, and inverting such a matrix is analytically possible by definition, but numerically unstable; rescaling the RHS variables alleviates this better than setting <code>tol.solve</code> to a very small value
<code>llprof</code>	default NULL, can either be an integer, to divide the feasible range into <code>llprof</code> points, or a sequence of spatial coefficient values, at which to evaluate the likelihood function
<code>control</code>	list of extra control arguments - see section below
<code>object</code>	<code>Spautolm</code> object from <code>spautolm</code>
<code>correlation</code>	logical; if 'TRUE', the correlation matrix of the estimated parameters is returned and printed (default=FALSE)
<code>adj.se</code>	if TRUE, adjust the coefficient standard errors for the number of fitted coefficients
<code>Nagelkerke</code>	if TRUE, the Nagelkerke pseudo R-squared is reported
<code>...</code>	further arguments passed to or from other methods

Details

This implementation is based on `lm.gls` and `errorsarlm`. In particular, the function does not (yet) prevent asymmetric spatial weights being used with "CAR" family models. It appears that both numerical issues (convergence in particular) and uncertainties about the exact spatial weights matrix used make it difficult to reproduce Cressie and Chan's 1989 results, also given in Cressie 1993.

Note that the `fitted()` function for the output object assumes that the response variable may be reconstructed as the sum of the trend, the signal, and the noise (residuals). Since the values of the response variable are known, their spatial lags are used to calculate signal components (Cressie 1993, p. 564). This differs from other software, including GeoDa, which does not use knowledge of the response variable in making predictions for the fitting data.

Value

A list object of class Spautolm:

fit	a list, with items: coefficients ML coefficient estimates SSE ML sum of squared errors s2 ML residual variance imat ML coefficient covariance matrix (before multiplying by s2) signal_trend non-spatial component of fitted.values signal_stochastic spatial component of fitted.values fitted.values sum of non-spatial and spatial components of fitted.values residuals difference between observed and fitted values
lambda	ML autoregressive coefficient
LL	log likelihood for fitted model
LL0	log likelihood for model with lambda=0
call	the call used to create this object
parameters	number of parameters estimated
aliased	if not NULL, details of aliased variables
method	Jacobian method chosen
family	family chosen
zero.policy	zero.policy used
weights	case weights used
interval	the line search interval used
timings	processing timings
na.action	(possibly) named vector of excluded or omitted observations if non-default na.action argument used
llprof	if not NULL, a list with components lambda and ll of equal length
lambda.se	Numerical Hessian-based standard error of lambda
fdHess	Numerical Hessian-based variance-covariance matrix
X	covariates used in model fitting
Y	response used in model fitting
weights	weights used in model fitting

Control arguments

tol.opt: the desired accuracy of the optimization - passed to optimize() (default=.Machine\$double.eps^(2/3))

fdHess: default NULL, then set to (method != "eigen") internally; use fdHess to compute an approximate Hessian using finite differences when using sparse matrix methods; used to make a coefficient covariance matrix when the number of observations is large; may be turned off to save resources if need be

- optimHess:** default FALSE, use fdHess from **nlme**, if TRUE, use optim to calculate Hessian at optimum
- optimHessMethod:** default “optimHess”, may be “nlm” or one of the optim methods
- Imult:** default 2; used for preparing the Cholesky decompositions for updating in the Jacobian function
- super:** if NULL (default), set to FALSE to use a simplicial decomposition for the sparse Cholesky decomposition and method “Matrix_J”, set to `as.logical(NA)` for method “Matrix”, if TRUE, use a supernodal decomposition
- cheb_q:** default 5; highest power of the approximating polynomial for the Chebyshev approximation
- MC_p:** default 16; number of random variates
- MC_m:** default 30; number of products of random variates matrix and spatial weights matrix
- type** default “MC”, used with method “moments”; alternatives “mult” and “moments”, for use if trs is missing, [trW](#)
- correct** default TRUE, used with method “moments” to compute the Smirnov/Anselin correction term
- trunc** default TRUE, used with method “moments” to truncate the Smirnov/Anselin correction term
- SE_method** default “LU”, may be “MC”
- nrho** default 200, as in SE toolbox; the size of the first stage Indet grid; it may be reduced to for example 40
- interpn** default 2000, as in SE toolbox; the size of the second stage Indet grid
- small_asy** default TRUE; if the method is not “eigen”, use asymmetric covariances rather than numerical Hessian ones if $n \leq \text{small}$
- small** default 1500; threshold number of observations for asymmetric covariances when the method is not “eigen”
- SEIndet** default NULL, may be used to pass a pre-computed SE toolbox style matrix of coefficients and their Indet values to the “SE_classic” and “SE_whichMin” methods
- LU_order** default FALSE; used in “LU_prepermute”, note warnings given for lu method
- pre_eig** default NULL; may be used to pass a pre-computed vector of eigenvalues

Note

The standard errors given in Waller and Gotway (2004) are adjusted for the numbers of parameters estimated, and may be reproduced by using the additional argument `adj.se=TRUE` in the summary method. In addition, the function returns fitted values and residuals as given by Cressie (1993) p. 564.

Author(s)

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References

Cliff, A. D., Ord, J. K. 1981 *Spatial processes*, Pion; Ord, J. K. 1975 Estimation methods for models of spatial interaction, *Journal of the American Statistical Association*, 70, 120-126; Waller, L. A., Gotway, C. A. 2004 *Applied spatial statistics for public health*, Wiley, Hoboken, NJ, 325-380; Cressie, N. A. C. 1993 *Statistics for spatial data*, Wiley, New York, 548-568; Ripley, B. D. 1981 *Spatial statistics*, Wiley, New York, 88-95; LeSage J and RK Pace (2009) *Introduction to Spatial Econometrics*. CRC Press, Boca Raton.

See Also

[optimize](#), [errorsarlm](#), [do_ldet](#)

Examples

```
require("sf", quietly=TRUE)
nydata <- st_read(system.file("shapes/NY8_bna_utm18.gpkg", package="spData")[1], quiet=TRUE)
## Not run:
lm0 <- lm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata)
summary(lm0)
lm0w <- lm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata, weights=POP8)
summary(lm0w)

## End(Not run)
suppressMessages(nyadjmat <- as.matrix(foreign::read.dbf(system.file(
  "misc/nyadjwts.dbf", package="spData")[1])[-1]))
suppressMessages(ID <- as.character(names(foreign::read.dbf(system.file(
  "misc/nyadjwts.dbf", package="spData")[1])[-1]))
identical(substring(ID, 2, 10), substring(as.character(nydata$AREAKEY), 2, 10))
#require("spdep", quietly=TRUE)
listw_NY <- spdep::mat2listw(nyadjmat, as.character(nydata$AREAKEY), style="B")
eigs <- eigenw(listw_NY)
## Not run:
esar0 <- errorsarlm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY)
summary(esar0)
system.time(esar1f <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME,
  data=nydata, listw=listw_NY, family="SAR", method="eigen",
  control=list(pre_eig=eigs)))
res <- summary(esar1f)
print(res)
coef(res)
sqrt(diag(res$resvar))
sqrt(diag(esar1f$fit$imat)*esar1f$fit$s2)
sqrt(diag(esar1f$fdHess))
system.time(esar1M <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME,
  data=nydata, listw=listw_NY, family="SAR", method="Matrix"))
summary(esar1M)
system.time(esar1M <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME,
  data=nydata, listw=listw_NY, family="SAR", method="Matrix",
  control=list(super=TRUE)))
summary(esar1M)
```

```

esar1wf <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, weights=POP8, family="SAR", method="eigen",
  control=list(pre_eig=eigs))
summary(esar1wf)
system.time(esar1wM <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME,
  data=nydata, listw=listw_NY, weights=POP8, family="SAR", method="Matrix"))
summary(esar1wM)
esar1wlu <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, weights=POP8, family="SAR", method="LU")
summary(esar1wlu)
esar1wch <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, weights=POP8, family="SAR", method="Chebyshev")
summary(esar1wch)

## End(Not run)
ecar1f <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, family="CAR", method="eigen",
  control=list(pre_eig=eigs))
summary(ecar1f)
## Not run:
system.time(ecar1M <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME,
  data=nydata, listw=listw_NY, family="CAR", method="Matrix"))
summary(ecar1M)

## End(Not run)
ecar1wf <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME, data=nydata,
  listw=listw_NY, weights=POP8, family="CAR", method="eigen",
  control=list(pre_eig=eigs))
summary(ecar1wf)
## Not run:
system.time(ecar1wM <- spautolm(Z ~ PEXPOSURE + PCTAGE65P + PCTOWNHOME,
  data=nydata, listw=listw_NY, weights=POP8, family="CAR", method="Matrix"))
summary(ecar1wM)

## End(Not run)
## Not run:
require("sf", quietly=TRUE)
nc.sids <- st_read(system.file("shapes/sids.gpkg", package="spData")[1], quiet=TRUE)
ft.SID74 <- sqrt(1000)*(sqrt(nc.sids$SID74/nc.sids$BIR74) +
  sqrt((nc.sids$SID74+1)/nc.sids$BIR74))
lm_nc <- lm(ft.SID74 ~ 1)
sids.nhbr30 <- spdep::dnearneigh(cbind(nc.sids$east, nc.sids$north), 0, 30,
  row.names=row.names(nc.sids))
sids.nhbr30.dist <- spdep::nbdists(sids.nhbr30, cbind(nc.sids$east, nc.sids$north))
sids.nhbr <- spdep::listw2sn(spdep::nb2listw(sids.nhbr30,
  glist=sids.nhbr30.dist, style="B", zero.policy=TRUE))
dij <- sids.nhbr[,3]
n <- nc.sids$BIR74
e11 <- min(dij)/dij
e12 <- sqrt(n[sids.nhbr$to]/n[sids.nhbr$from])
sids.nhbr$weights <- e11*e12
sids.nhbr.listw <- spdep::sn2listw(sids.nhbr)
both <- factor(paste(nc.sids$L_id, nc.sids$M_id, sep=":"))

```

```

ft.NWBIR74 <- sqrt(1000)*(sqrt(nc.sids$NWBIR74/nc.sids$BIR74) +
  sqrt((nc.sids$NWBIR74+1)/nc.sids$BIR74))
mdata <- data.frame(both, ft.NWBIR74, ft.SID74, BIR74=nc.sids$BIR74)
outl <- which.max(rstandard(lm_nc))
as.character(nc.sids$NAME[outl])
mdata.4 <- mdata[-outl,]
W <- spdep::listw2mat(sids.nhbr.listw)
W.4 <- W[-outl, -outl]
sids.nhbr.listw.4 <- spdep::mat2listw(W.4)
esarI <- errorsarlm(ft.SID74 ~ 1, data=mdata, listw=sids.nhbr.listw,
  zero.policy=TRUE)
summary(esarI)
esarIa <- spautolm(ft.SID74 ~ 1, data=mdata, listw=sids.nhbr.listw,
  family="SAR")
summary(esarIa)
esarIV <- errorsarlm(ft.SID74 ~ ft.NWBIR74, data=mdata, listw=sids.nhbr.listw,
  zero.policy=TRUE)
summary(esarIV)
esarIVa <- spautolm(ft.SID74 ~ ft.NWBIR74, data=mdata, listw=sids.nhbr.listw,
  family="SAR")
summary(esarIVa)
esarIaw <- spautolm(ft.SID74 ~ 1, data=mdata, listw=sids.nhbr.listw,
  weights=BIR74, family="SAR")
summary(esarIaw)
esarIIaw <- spautolm(ft.SID74 ~ both - 1, data=mdata, listw=sids.nhbr.listw,
  weights=BIR74, family="SAR")
summary(esarIIaw)
esarIVaw <- spautolm(ft.SID74 ~ ft.NWBIR74, data=mdata,
  listw=sids.nhbr.listw, weights=BIR74, family="SAR")
summary(esarIVaw)
ecarIaw <- spautolm(ft.SID74 ~ 1, data=mdata.4, listw=sids.nhbr.listw.4,
  weights=BIR74, family="CAR")
summary(ecarIaw)
ecarIIaw <- spautolm(ft.SID74 ~ both - 1, data=mdata.4,
  listw=sids.nhbr.listw.4, weights=BIR74, family="CAR")
summary(ecarIIaw)
ecarIVaw <- spautolm(ft.SID74 ~ ft.NWBIR74, data=mdata.4,
  listw=sids.nhbr.listw.4, weights=BIR74, family="CAR")
summary(ecarIVaw)
nc.sids$fitIV <- append(fitted.values(ecarIVaw), NA, outl-1)
plot(nc.sids[, "fitIV"], nbreaks=12) # Cressie 1993, p. 565

## End(Not run)
## Not run:
data(oldcol, package="spdep")
COL.errW.eig <- errorsarlm(CRIME ~ INC + HOVAL, data=COL.OLD,
  spdep::nb2listw(COL.nb, style="W"))
summary(COL.errW.eig)
COL.errW.sar <- spautolm(CRIME ~ INC + HOVAL, data=COL.OLD,
  spdep::nb2listw(COL.nb, style="W"))
summary(COL.errW.sar)
data(boston, package="spData")
gp1 <- spautolm(log(CMEDV) ~ CRIM + ZN + INDUS + CHAS + I(NOX^2)

```

```

+ I(RM^2) + AGE + log(DIS) + log(RAD) + TAX + PTRATIO + B + log(LSTAT),
data=boston.c, spdep::nb2listw(boston.soi), family="SMA")
summary(gp1)

## End(Not run)

```

spBreg_lag	<i>Bayesian MCMC spatial simultaneous autoregressive model estimation</i>
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Description

The `spBreg_lag` function is an early-release version of the Matlab Spatial Econometrics Toolbox function `sar_g.m`, using drawing by inversion, and not accommodating heteroskedastic disturbances.

Usage

```

spBreg_lag(formula, data = list(), listw, na.action, Durbin, type,
  zero.policy=NULL, control=list())
spBreg_sac(formula, data = list(), listw, listw2=NULL, na.action,
  Durbin, type, zero.policy=NULL, control=list())
spBreg_err(formula, data = list(), listw, na.action, Durbin, etype,
  zero.policy=NULL, control=list())
## S3 method for class 'MCMC_sar_G'
impacts(obj, ..., tr=NULL, listw=NULL, evalues=NULL, Q=NULL)
## S3 method for class 'MCMC_sem_G'
impacts(obj, ..., tr=NULL, listw=NULL, evalues=NULL, Q=NULL)
## S3 method for class 'MCMC_sac_G'
impacts(obj, ..., tr=NULL, listw=NULL, evalues=NULL, Q=NULL)

```

Arguments

<code>formula</code>	a symbolic description of the model to be fit. The details of model specification are given for <code>lm()</code>
<code>data</code>	an optional data frame containing the variables in the model. By default the variables are taken from the environment which the function is called.
<code>listw, listw2</code>	a <code>listw</code> object created for example by <code>nb2listw</code>
<code>na.action</code>	a function (default <code>options("na.action")</code>), can also be <code>na.omit</code> or <code>na.exclude</code> with consequences for residuals and fitted values - in these cases the weights list will be subsetted to remove NAs in the data. It may be necessary to set <code>zero.policy</code> to <code>TRUE</code> because this subsetting may create no-neighbour observations. Note that only weights lists created without using the <code>glist</code> argument to <code>nb2listw</code> may be subsetted.
<code>Durbin</code>	default <code>FALSE</code> (spatial lag model); if <code>TRUE</code> , full spatial Durbin model; if a formula object, the subset of explanatory variables to lag

type, etype	(use the ‘Durbin=’ argument - retained for backwards compatibility only) default "lag", may be set to "mixed"; when "mixed", the lagged intercept is dropped for spatial weights style "W", that is row-standardised weights, but otherwise included; “Durbin” may be used instead of “mixed”
zero.policy	default NULL, use global option value; if TRUE assign zero to the lagged value of zones without neighbours, if FALSE (default) assign NA
control	list of extra control arguments - see section below
obj	A spatial regression object
...	Arguments passed through to methods in the coda package
tr	A vector of traces of powers of the spatial weights matrix created using trW, for approximate impact measures; if not given, listw must be given for exact measures (for small to moderate spatial weights matrices); the traces must be for the same spatial weights as were used in fitting the spatial regression, and must be row-standardised
evalues	vector of eigenvalues of spatial weights matrix for impacts calculations
Q	default NULL, else an integer number of cumulative power series impacts to calculate if tr is given

Control arguments

- tol.opt:** the desired accuracy of the optimization - passed to `optimize()` (default=square root of double precision machine tolerance, a larger root may be used needed, see `help(boston)` for an example)
- fdHess:** default NULL, then set to (method != "eigen") internally; use `fdHess` to compute an approximate Hessian using finite differences when using sparse matrix methods; used to make a coefficient covariance matrix when the number of observations is large; may be turned off to save resources if need be
- optimHess:** default FALSE, use `fdHess` from **nlme**, if TRUE, use `optim` to calculate Hessian at optimum
- optimHessMethod:** default “optimHess”, may be “nlm” or one of the `optim` methods
- compiled_sse:** default FALSE; logical value used in the log likelihood function to choose compiled code for computing SSE
- Imult:** default 2; used for preparing the Cholesky decompositions for updating in the Jacobian function
- super:** if NULL (default), set to FALSE to use a simplicial decomposition for the sparse Cholesky decomposition and method “Matrix_J”, set to `as.logical(NA)` for method “Matrix”, if TRUE, use a supernodal decomposition
- cheb_q:** default 5; highest power of the approximating polynomial for the Chebyshev approximation
- MC_p:** default 16; number of random variates
- MC_m:** default 30; number of products of random variates matrix and spatial weights matrix
- spamPivot:** default “MMD”, alternative “RCM”
- in_coef** default 0.1, coefficient value for initial Cholesky decomposition in “spam_update”

- type** default “MC”, used with method “moments”; alternatives “mult” and “moments”, for use if trs is missing, `trW`
- correct** default TRUE, used with method “moments” to compute the Smirnov/Anselin correction term
- trunc** default TRUE, used with method “moments” to truncate the Smirnov/Anselin correction term
- SE_method** default “LU”, may be “MC”
- nrho** default 200, as in SE toolbox; the size of the first stage Indet grid; it may be reduced to for example 40
- interpn** default 2000, as in SE toolbox; the size of the second stage Indet grid
- small_asy** default TRUE; if the method is not “eigen”, use asymmetric covariances rather than numerical Hessian ones if $n \leq \text{small}$
- small** default 1500; threshold number of observations for asymmetric covariances when the method is not “eigen”
- SEIndet** default NULL, may be used to pass a pre-computed SE toolbox style matrix of coefficients and their Indet values to the “SE_classic” and “SE_whichMin” methods
- LU_order** default FALSE; used in “LU_prepermute”, note warnings given for lu method
- pre_eig** default NULL; may be used to pass a pre-computed vector of eigenvalues
- OrdVsign** default 1; used to set the sign of the final component to negative if -1 (alpha times ((sigma squared) squared) in Ord (1975) equation B.1).

Extra Bayesian control arguments

- ldet_method** default “SE_classic”; equivalent to the method argument in `lagsarlm`
- interval** default $c(-1, 1)$; used unmodified or set internally by `jacobianSetup`
- ndraw** default 2500L; integer total number of draws
- nomit** default 500L; integer total number of omitted burn-in draws
- thin** default 1L; integer thinning proportion
- verbose** default FALSE; inverse of `quiet` argument in `lagsarlm`
- detval** default NULL; not yet in use, precomputed matrix of log determinants
- prior** a list with the following components:
- rhoMH, lambdaMH** default FALSE; use Metropolis or griddy Gibbs
 - Tbeta** default NULL; values of the betas variance-covariance matrix, set to $\text{diag}(k) * 1e+12$ if NULL
 - c_beta** default NULL; values of the betas set to 0 if NULL
 - rho** default 0.5; value of the autoregressive coefficient
 - sige** default 1; value of the residual variance
 - nu** default 0; informative $\text{Gamma}(\text{nu}, \text{d0})$ prior on `sige`
 - d0** default 0; informative $\text{Gamma}(\text{nu}, \text{d0})$ prior on `sige`
 - a1** default 1.01; parameter for $\text{beta}(a1, a2)$ prior on `rho`
 - a2** default 1.01; parameter for $\text{beta}(a1, a2)$ prior on `rho`

cc default 0.2; initial tuning parameter for M-H sampling
gG_sige default TRUE; include sige in lambda griddy Gibbs update
cc1 default 0.2; initial tuning parameter for M-H sampling
cc2 default 0.2; initial tuning parameter for M-H sampling

Author(s)

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References

LeSage J and RK Pace (2009) Introduction to Spatial Econometrics. CRC Press, Boca Raton.

Examples

```
#require("spdep", quietly=TRUE)
data(oldcol, package="spdep")
lw <- spdep::nb2listw(COL.nb, style="W")
require("coda", quietly=TRUE)
set.seed(1)
COL.err.Bayes <- spBreg_err(CRIME ~ INC + HOVAL, data=COL.OLD, listw=lw)
print(summary(COL.err.Bayes))
print(raftery.diag(COL.err.Bayes, r=0.01))
## Not run:
ev <- eigenw(lw)
W <- as(lw, "CsparseMatrix")
trMatc <- trW(W, type="mult")
set.seed(1)
COL.err.Bayes <- spBreg_err(CRIME ~ INC + HOVAL, data=COL.OLD, listw=lw,
  control=list(prior=list(lambdaMH=TRUE)))
print(summary(COL.err.Bayes))
print(raftery.diag(COL.err.Bayes, r=0.01))
set.seed(1)
COL.err.Bayes <- spBreg_err(CRIME ~ INC + HOVAL, data=COL.OLD, listw=lw,
  Durbin=TRUE)
print(summary(COL.err.Bayes))
print(summary(impacts(COL.err.Bayes)))
print(raftery.diag(COL.err.Bayes, r=0.01))
set.seed(1)
COL.err.Bayes <- spBreg_err(CRIME ~ INC + HOVAL, data=COL.OLD, listw=lw,
  Durbin=TRUE, control=list(prior=list(lambdaMH=TRUE)))
print(summary(COL.err.Bayes))
print(summary(impacts(COL.err.Bayes)))
print(raftery.diag(COL.err.Bayes, r=0.01))
set.seed(1)
COL.err.Bayes <- spBreg_err(CRIME ~ INC + HOVAL, data=COL.OLD, listw=lw,
  Durbin=~INC)
print(summary(COL.err.Bayes))
print(summary(impacts(COL.err.Bayes)))
print(raftery.diag(COL.err.Bayes, r=0.01))
set.seed(1)
```

```

COL.err.Bayes <- spBreg_err(CRIME ~ INC + HOVAL, data=COL.OLD, listw=lw,
  Durbin=~INC, control=list(prior=list(lambdaMH=TRUE)))
print(summary(COL.err.Bayes))
print(summary(impacts(COL.err.Bayes)))
print(raftery.diag(COL.err.Bayes, r=0.01))
set.seed(1)
COL.sacW.B0 <- spBreg_sac(CRIME ~ INC + HOVAL, data=COL.OLD, listw=lw,
  Durbin=FALSE, control=list(ndraw=1500L, nomit=500L))
print(summary(COL.sacW.B0))
print(summary(impacts(COL.sacW.B0, tr=trMatc), zstats=TRUE, short=TRUE))
set.seed(1)
COL.sacW.B1 <- spBreg_sac(CRIME ~ INC + HOVAL, data=COL.OLD, listw=lw,
  Durbin=TRUE, control=list(ndraw=1500L, nomit=500L))
print(summary(COL.sacW.B1))
print(summary(impacts(COL.sacW.B1, tr=trMatc), zstats=TRUE, short=TRUE))
set.seed(1)
COL.lag.Bayes <- spBreg_lag(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw=lw)
print(summary(COL.lag.Bayes))
print(summary(impacts(COL.lag.Bayes, tr=trMatc), short=TRUE, zstats=TRUE))
print(summary(impacts(COL.lag.Bayes, evalues=ev), short=TRUE, zstats=TRUE))
set.seed(1)
COL.D0.Bayes <- spBreg_lag(CRIME ~ INC + HOVAL, data=COL.OLD,
  listw=lw, Durbin=TRUE)
print(summary(COL.D0.Bayes))
print(summary(impacts(COL.D0.Bayes, tr=trMatc), short=TRUE, zstats=TRUE))
set.seed(1)
COL.D1.Bayes <- spBreg_lag(CRIME ~ DISCBD + INC + HOVAL, data=COL.OLD,
  listw=lw, Durbin=~ INC)
print(summary(COL.D1.Bayes))
print(summary(impacts(COL.D1.Bayes, tr=trMatc), short=TRUE, zstats=TRUE))
#data(elect80, package="spData")
#lw <- spdep::nb2listw(e80_queen, zero.policy=TRUE)
#el_ml <- lagsarlm(log(pc_turnout) ~ log(pc_college) + log(pc_homeownership)
# + log(pc_income), data=elect80, listw=lw, zero.policy=TRUE, method="LU")
#print(summary(el_ml))
#set.seed(1)
#el_B <- spBreg_lag(log(pc_turnout) ~ log(pc_college) + log(pc_homeownership)
# + log(pc_income), data=elect80, listw=lw, zero.policy=TRUE)
#print(summary(el_B))
#print(el_ml$timings)
#print(attr(el_B, "timings"))

## End(Not run)

```

Description

The function fits a spatial lag model by two stage least squares, with the option of adjusting the results for heteroskedasticity.

Usage

```
stsls(formula, data = list(), listw, zero.policy = NULL,
      na.action = na.fail, robust = FALSE, HC=NULL, legacy=FALSE, W2X = TRUE,
      sig2n_k=TRUE, adjust.n=FALSE)
## S3 method for class 'Stsls'
impacts(obj, ..., tr, R = NULL, listw = NULL, evalues=NULL,
        tol = 1e-06, empirical = FALSE, Q=NULL)
```

Arguments

formula	a symbolic description of the model to be fit. The details of model specification are given for <code>lm()</code>
data	an optional data frame containing the variables in the model. By default the variables are taken from the environment which the function is called.
listw	a <code>listw</code> object created for example by <code>nb2listw</code>
zero.policy	default <code>NULL</code> , use global option value; if <code>TRUE</code> assign zero to the lagged value of zones without neighbours, if <code>FALSE</code> (default) assign <code>NA</code> - causing <code>lagsarlm()</code> to terminate with an error
na.action	a function (default <code>na.fail</code>), can also be <code>na.omit</code> or <code>na.exclude</code> with consequences for residuals and fitted values - in these cases the weights list will be subsetted to remove <code>NA</code> s in the data. It may be necessary to set <code>zero.policy</code> to <code>TRUE</code> because this subsetting may create no-neighbour observations. Note that only weights lists created without using the <code>glist</code> argument to <code>nb2listw</code> may be subsetted.
robust	default <code>FALSE</code> , if <code>TRUE</code> , apply a heteroskedasticity correction to the coefficients covariances
HC	default <code>NULL</code> , if <code>robust</code> is <code>TRUE</code> , assigned “ <code>HC0</code> ”, may take values “ <code>HC0</code> ” or “ <code>HC1</code> ” for White estimates or MacKinnon-White estimates respectively
legacy	the argument chooses between two implementations of the robustness correction: default <code>FALSE</code> - use the estimate of Omega only in the White consistent estimator of the variance-covariance matrix, if <code>TRUE</code> , use the original implementation which runs a GLS using the estimate of Omega, overrides <code>sig2n_k</code> , and yields different coefficient estimates as well - see example below
W2X	default <code>TRUE</code> , if <code>FALSE</code> only <code>WX</code> are used as instruments in the spatial two stage least squares; until release 0.4-60, only <code>WX</code> were used - see example below; Python <code>sprege::GM_Lag</code> is default <code>FALSE</code>
sig2n_k	default <code>TRUE</code> - use <code>n-k</code> to calculate σ^2 , if <code>FALSE</code> use <code>n</code> ; Python <code>sprege::GM_Lag</code> is default <code>FALSE</code>
adjust.n	default <code>FALSE</code> , used in creating spatial weights constants for the Anselin-Kelejian (1997) test

obj	A spatial regression object created by <code>lagsarlm</code> , <code>lagmess</code> or by <code>lmSLX</code> ; in <code>HPDinterval.LagImpact</code> , a <code>LagImpact</code> object
...	Arguments passed through to methods in the cod a package
tr	A vector of traces of powers of the spatial weights matrix created using <code>trW</code> , for approximate impact measures; if not given, <code>listw</code> must be given for exact measures (for small to moderate spatial weights matrices); the traces must be for the same spatial weights as were used in fitting the spatial regression, and must be row-standardised
evalues	vector of eigenvalues of spatial weights matrix for impacts calculations
R	If given, simulations are used to compute distributions for the impact measures, returned as <code>mcmc</code> objects; the objects are used for convenience but are not output by an MCMC process
tol	Argument passed to <code>mvrnorm</code> : tolerance (relative to largest variance) for numerical lack of positive-definiteness in the coefficient covariance matrix
empirical	Argument passed to <code>mvrnorm</code> (default <code>FALSE</code>): if true, the coefficients and their covariance matrix specify the empirical not population mean and covariance matrix
Q	default <code>NULL</code> , else an integer number of cumulative power series impacts to calculate if <code>tr</code> is given

Details

The fitting implementation fits a spatial lag model:

$$y = \rho W y + X\beta + \varepsilon$$

by using spatially lagged X variables as instruments for the spatially lagged dependent variable.

From version 1.3-6, the general Anselin-Kelejian (1997) test for residual spatial autocorrelation is added.

Value

an object of class "Stsls" containing:

coefficients	coefficient estimates
var	coefficient covariance matrix
sse	sum of squared errors
residuals	model residuals
df	degrees of freedom

Author(s)

Luc Anselin, Gianfranco Piras and Roger Bivand

References

- Kelejian, H.H. and I.R. Prucha (1998). A generalized spatial two stage least squares procedure for estimating a spatial autoregressive model with autoregressive disturbances. *Journal of Real Estate Finance and Economics* 17, 99-121. doi:10.1023/A:1007707430416.
- Anselin, L., & Kelejian, H. H. (1997). Testing for Spatial Error Autocorrelation in the Presence of Endogenous Regressors. *International Regional Science Review*, 20(1-2), 153-182. doi:10.1177/016001769702000109.
- Roger Bivand, Gianfranco Piras (2015). Comparing Implementations of Estimation Methods for Spatial Econometrics. *Journal of Statistical Software*, 63(18), 1-36. doi:10.18637/jss.v063.i18.

See Also

[lagsarlm](#)

Examples

```
data(oldcol, package="spdep")
#require(spdep, quietly=TRUE)
lw <- spdep::nb2listw(COL.nb)
COL.lag.eig <- lagsarlm(CRIME ~ INC + HOVAL, data=COL.OLD, lw)
summary(COL.lag.eig, correlation=TRUE)
COL.lag.stsls <- stsls(CRIME ~ INC + HOVAL, data=COL.OLD, lw)
(x <- summary(COL.lag.stsls, correlation=TRUE))
coef(x)
W <- as(lw, "CsparseMatrix")
trMatc <- trW(W, type="mult")
loobj1 <- impacts(COL.lag.stsls, R=200, tr=trMatc)
summary(loobj1, zstats=TRUE, short=TRUE)
ev <- eigenw(lw)
loobj2 <- impacts(COL.lag.stsls, R=200, evalues=ev)
summary(loobj2, zstats=TRUE, short=TRUE)
require(coda)
HPDinterval(loobj1)
COL.lag.stslsW <- stsls(CRIME ~ INC + HOVAL, data=COL.OLD, lw, W2X=FALSE)
summary(COL.lag.stslsW, correlation=TRUE)
COL.lag.stslsWn <- stsls(CRIME ~ INC + HOVAL, data=COL.OLD, lw, W2X=FALSE, sig2n_k=FALSE)
summary(COL.lag.stslsWn, correlation=TRUE)
COL.lag.stslsR <- stsls(CRIME ~ INC + HOVAL, data=COL.OLD, lw,
robust=TRUE, W2X=FALSE)
summary(COL.lag.stslsR, correlation=TRUE)
COL.lag.stslsRl <- stsls(CRIME ~ INC + HOVAL, data=COL.OLD, lw,
robust=TRUE, legacy=TRUE, W2X=FALSE)
summary(COL.lag.stslsRl, correlation=TRUE)
data(boston, package="spData")
gp2a <- stsls(log(CMEDV) ~ CRIM + ZN + INDUS + CHAS + I(NOX^2) + I(RM^2) +
AGE + log(DIS) + log(RAD) + TAX + PTRATIO + B + log(LSTAT),
data=boston.c, spdep::nb2listw(boston.soi))
summary(gp2a)
```


Author(s)

Roger Bivand <Roger.Bivand@nhh.no>

References

LeSage J and RK Pace (2009) *Introduction to Spatial Econometrics*. CRC Press, Boca Raton, pp. 96–105; Smirnov O and L Anselin (2009) An O(N) parallel method of computing the Log-Jacobian of the variable transformation for models with spatial interaction on a lattice. *Computational Statistics and Data Analysis* 53 (2009) 2983–2984.

See Also

[as_dgRMatrix_listw](#), [nb2listw](#)

Examples

```
require("sf", quietly=TRUE)
columbus <- st_read(system.file("shapes/columbus.gpkg", package="spData")[1], quiet=TRUE)
#require(spdep, quietly=TRUE)
col.gal.nb <- spdep::read.gal(system.file("weights/columbus.gal", package="spData")[1])
listw <- spdep::nb2listw(col.gal.nb)
W <- as(listw, "CsparseMatrix")
system.time(trMat <- trW(W, type="mult"))
str(trMat)
set.seed(1100)
system.time(trMC <- trW(W, type="MC"))
str(trMC)
plot(trMat, trMC)
abline(a=0, b=1)
for(i in 3:length(trMC)) {
  segments(trMat[i], trMC[i]-2*attr(trMC, "sd")[i], trMat[i],
    trMC[i]+2*attr(trMC, "sd")[i])
}
listwS <- similar.listw(listw)
W <- forceSymmetric(as(listwS, "CsparseMatrix"))
system.time(trmom <- trW(listw=listwS, m=24, type="moments"))
str(trmom)
all.equal(trMat[1:24], trmom, check.attributes=FALSE)
system.time(trMat <- trW(W, m=24, type="mult"))
str(trMat)
all.equal(trMat, trmom, check.attributes=FALSE)
set.seed(1)
system.time(trMC <- trW(W, m=24, type="MC"))
str(trMC)
## Not run:
data(boston, package="spData")
listw <- spdep::nb2listw(boston.soi)
listwS <- similar.listw(listw)
system.time(trmom <- trW(listw=listwS, m=24, type="moments"))
str(trmom)
library(parallel)
nc <- max(2L, detectCores(logical=FALSE), na.rm = TRUE)-1L
```

```
# set nc to 1L here
if (nc > 1L) nc <- 1L
coresOpt <- get.coresOption()
invisible(set.coresOption(nc))
if(!get.mcOption()) {
  cl <- makeCluster(get.coresOption())
  set.ClusterOption(cl)
}
system.time(trmomp <- trW(listw=listwS, m=24, type="moments"))
if(!get.mcOption()) {
  set.ClusterOption(NULL)
  stopCluster(cl)
}
all.equal(trmom, trmomp, check.attributes=FALSE)
invisible(set.coresOption(coresOpt))

## End(Not run)
```

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